

## Sensing Tree Automata as a Model of Syntactic Dependencies

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### The Talk in One Minute

#### The research program

a tight upper bound to the complexity of natural language dependencies?

#### In this talk

- Sensing tree automata as a uniform upper bound
- MG dependency trees

### Spoilers

- A (linguistically) natural perspective!
- Empirically attested restrictions on movement
- Head-argument relations
- C-command and licensing conditions

### Outline

1 Preliminaries

- 2 Merge and Move via STA
- **3** Licensing Conditions
- **4** Conclusion & Open Questions

### Computational Theories of Language

#### The subregular program

Can we provide tight complexity characterizations for natural language?

 Particularly successful in phonology (Heinz et al. 2011; Chandlee 2014; Jardine 2016; McMullin 2016; Graf 2017; Graf and Mayer 2018)

#### Some results for syntax

- regular tree languages (Michaelis 2004; Kobele et al. 2007; Graf 2012)
- subregular operations? (Graf 2012, 2018)
- subregular dependencies? (Vu 2018; Vu et al. 2019)
- subregular constraints? (Shafiei and Graf 2019)

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#### Can we gain a unified perspective for syntax?

Syntax?

#### We need a formal model of syntactic structures.

 Minimalist grammars (MGs) are a formalization of Minimalist syntax. (Stabler 1997, 2011)

Operations:

Merge

category feature  $\mathrm{N}^-,\,\mathrm{D}^-,\,\ldots$  selector feature  $\mathrm{N}^+,\,\mathrm{D}^+,\,\ldots$ 

Move

licensee feature  $wh^-$ ,  $nom^-$ , ... licensor feature  $wh^+$ ,  $nom^+$ , ...

- Adopt Chomsky-Borer hypothesis: Grammar is just a finite list of feature-annotated lexical items
- The set of derivation trees is a regular tree language. (Michaelis 2004; Kobele et al. 2007; Graf 2012)

### MG Syntax: Derivation Trees





Phrase Structure Tree

**Derivation Tree** 

### MG Syntax: Dependency Trees



**Derivation Tree** 

**Dependency Tree** 

Sensing Tree Automaton (Martens 2006)

Deterministic top-down tree automaton with finite look-ahead of 1.



▶ 
$$0(b) \rightarrow b; 1(b) \rightarrow b$$
  
▶  $1(a) \rightarrow a$ 

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Interim Summary

#### We are looking for a complexity upper bound for syntax...

- MG dependency trees (MDEP)
- STA

#### Upcoming

- ▶ MDEP[*merge*]  $\subseteq$  STA
- ▶ MDEP[*merge*,*move*] ⊊ STA iff we restrict *move*

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$$\varepsilon ::: T^+ C^- \langle T^+ \rangle$$

$$i \in :: V^+ T^- \langle V^+ \rangle$$
likes :: D^+ D^+ V^-
a :: N<sup>+</sup> D<sup>-</sup> the :: N<sup>+</sup> D<sup>-</sup>  
teacher :: P<sup>+</sup> N<sup>-</sup> father :: P<sup>+</sup> N<sup>-</sup>  
of :: D<sup>+</sup> P<sup>-</sup> of :: D<sup>+</sup> P<sup>-</sup>  
|  
Paul :: D<sup>-</sup> John :: D<sup>-</sup>

$$\varepsilon :: \mathbf{T}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \rangle$$

$$\varepsilon :: \mathbf{V}^{+} \mathbf{T}^{-} \langle \mathbf{V}^{+} \rangle$$

$$\downarrow$$
likes ::  $\mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \rangle$ 

$$\downarrow$$
a ::  $\mathbf{N}^{+} \mathbf{D}^{-}$  the ::  $\mathbf{N}^{+} \mathbf{D}^{-} \langle \mathbf{N}^{+} \rangle$ 
teacher ::  $\mathbf{P}^{+} \mathbf{N}^{-}$  father ::  $\mathbf{P}^{+} \mathbf{N}^{-}$ 

$$\downarrow$$
of ::  $\mathbf{D}^{+} \mathbf{P}^{-}$  of ::  $\mathbf{D}^{+} \mathbf{P}^{-}$ 

$$\downarrow$$
Paul ::  $\mathbf{D}^{-}$  John ::  $\mathbf{D}^{-}$ 

$$\varepsilon :: \mathbf{T}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \rangle$$

$$\varepsilon :: \mathbf{V}^{+} \mathbf{T}^{-} \langle \mathbf{V}^{+} \rangle$$

$$\stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \frac{\langle \mathbf{D}^{+} \mathbf{D}^{+} \rangle}{\langle \mathbf{P}^{+} \rangle}$$

$$\stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \langle \mathbf{N}^{+} \rangle$$

$$\stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{+}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{+}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{+}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{+}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{-}}} \stackrel{|}{\underset{\mathbf{N}^{+} \mathbf{D}^{$$

$$\begin{array}{c} \varepsilon :: \ \mathbf{T}^+ \ \mathbf{C}^- \ \left\langle \mathbf{T}^+ \right\rangle \\ & i \\ \varepsilon :: \ \mathbf{V}^+ \ \mathbf{T}^- \ \left\langle \mathbf{V}^+ \right\rangle \\ & i \\ \text{likes} :: \ \mathbf{D}^+ \ \mathbf{D}^+ \ \mathbf{V}^- \ \left\langle \mathbf{D}^+ \mathbf{D}^+ \right\rangle \\ & \mathbf{V}^+ \right\rangle \\ \mathbf{V}^+ \mathbf{V} \quad \mathbf{A} :: \ \mathbf{N}^+ \ \mathbf{D}^- \qquad \text{the} :: \ \mathbf{N}^+ \ \mathbf{D}^- \ \left\langle \mathbf{N}^+ \right\rangle \\ & \mathbf{V}^+ \right\rangle \\ \mathbf{V}^+ \mathbf{V} \quad \text{teacher} :: \ \mathbf{P}^+ \ \mathbf{N}^- \qquad \text{father} :: \ \mathbf{P}^+ \ \mathbf{N}^- \ \left\langle \mathbf{P}^+ \right\rangle \\ & i \\ \mathbf{V}^+ \right\rangle \quad \text{of} :: \ \mathbf{D}^+ \ \mathbf{P}^- \qquad \text{of} :: \ \mathbf{D}^+ \ \mathbf{P}^- \ \left\langle \mathbf{D}^+ \right\rangle \\ & i \\ \mathbf{P}aul :: \ \mathbf{D}^- \qquad \text{John} :: \ \mathbf{D}^- \end{array}$$

$$\varepsilon :: \mathbf{T}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \rangle$$

$$\varepsilon :: \mathbf{V}^{+} \mathbf{T}^{-} \langle \mathbf{V}^{+} \rangle$$

$$\stackrel{|}{\text{likes}} :: \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \rangle$$

$$\stackrel{|}{\langle \mathbf{N}^{+} \rangle} a :: \mathbf{N}^{+} \mathbf{D}^{-} \text{ the } :: \mathbf{N}^{+} \mathbf{D}^{-} \langle \mathbf{N}^{+} \rangle$$

$$\stackrel{|}{\langle \mathbf{P}^{+} \rangle} \text{ teacher } :: \mathbf{P}^{+} \mathbf{N}^{-} \text{ father } :: \mathbf{P}^{+} \mathbf{N}^{-} \langle \mathbf{P}^{+} \rangle$$

$$\stackrel{|}{\langle \mathbf{D}^{+} \rangle} \text{ of } :: \mathbf{D}^{+} \mathbf{P}^{-} \text{ of } :: \mathbf{D}^{+} \mathbf{P}^{-} \langle \mathbf{D}^{+} \rangle$$

$$\stackrel{|}{\langle \varepsilon \rangle} \text{ Paul } :: \mathbf{D}^{-} \text{ John } :: \mathbf{D}^{-} \langle \varepsilon \rangle$$

### MDEP[merge,move]


## MDEP[merge,move]



## MDEP[merge,move]













$$\varepsilon :: \mathbf{T}^{+} \mathbf{wh}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \mathbf{wh}^{+} \rangle$$

$$\varepsilon :: \mathbf{V}^{+} \mathbf{T}^{-} \langle \mathbf{V} \mathbf{wh}^{++} \rangle$$

$$| \mathbf{ke} :: \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{W}^{+} \rangle \mathbf{a} :: \mathbf{N}^{+} \mathbf{D}^{-} \quad \text{the } :: \mathbf{N}^{+} \mathbf{D}^{-} \langle \mathbf{N}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{W}^{+} \rangle \mathbf{teacher} :: \mathbf{P}^{+} \mathbf{N}^{-} \quad \text{father } :: \mathbf{P}^{+} \mathbf{N}^{-} \langle \mathbf{P}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{W}^{+} \rangle \mathbf{of} :: \mathbf{D}^{+} \mathbf{P}^{-} \quad \text{of } :: \mathbf{D}^{+} \mathbf{P}^{-} \langle \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{U}^{+} \rangle \mathbf{u} = \mathbf{U}^{-} \mathbf{u}^{+} \mathbf{u}^{+} \rangle$$

$$| \mathbf{U}^{-} \mathbf{U}^{+} \mathbf{wh}^{-} \mathbf{u}^{-} \mathbf{u}^{+} \mathbf{u}^{+} \rangle$$

$$\varepsilon :: \mathbf{T}^{+} \mathbf{wh}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \mathbf{wh}^{+} \rangle$$

$$\varepsilon :: \mathbf{V}^{+} \mathbf{T}^{-} \langle \mathbf{V} \mathbf{wh}^{++} \rangle$$

$$| \mathbf{ke} :: \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{W}^{+} \rangle \mathbf{a} :: \mathbf{N}^{+} \mathbf{D}^{-} \quad \text{the :: } \mathbf{N}^{+} \mathbf{D}^{-} \langle \mathbf{N}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{P}^{+} \rangle \text{ teacher :: } \mathbf{P}^{+} \mathbf{N}^{-} \quad \text{father :: } \mathbf{P}^{+} \mathbf{N}^{-} \langle \mathbf{P}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{P}^{+} \rangle \text{ of :: } \mathbf{D}^{+} \mathbf{P}^{-} \quad \text{of :: } \mathbf{D}^{+} \mathbf{P}^{-} \langle \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{E}^{+} \rangle \text{ is in } \mathbf{D}^{-} \text{ who :: } \mathbf{D}^{-} \text{ who :: } \mathbf{E}^{-} \rangle$$

t

# $\mathsf{MDEP}[\mathsf{merge},\mathsf{move}] \nsubseteq \mathsf{STA}$

$$\varepsilon :: \mathbf{T}^{+} \mathbf{wh}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \mathbf{wh}^{+} \rangle$$

$$\varepsilon :: \mathbf{V}^{+} \mathbf{T}^{-} \langle \mathbf{V} \mathbf{wh}^{++} \rangle$$

$$| \mathbf{ke} :: \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{ke} :: \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{vh}^{+} \mathbf{vh}^{+} \rangle \text{ teacher } :: \mathbf{P}^{+} \mathbf{N}^{-} \text{ the } :: \mathbf{N}^{+} \mathbf{D}^{-} \langle \mathbf{N}^{+} \rangle$$

$$| \mathbf{vh}^{+} \mathbf{vh}^{+} \rangle \text{ teacher } :: \mathbf{P}^{+} \mathbf{N}^{-} \text{ father } :: \mathbf{P}^{+} \mathbf{N}^{-} \langle \mathbf{P}^{+} \rangle$$

$$| \mathbf{vh}^{+} \mathbf{vh}^{-} \mathbf{vh}^{+} \mathbf{vh}^{-} \mathbf{vh}^{-} \mathbf{vh}^{+} \rangle$$

$$| \mathbf{vh}^{+} \mathbf{vh}^{-} \mathbf{vh}^{+} \mathbf{vh}^{-} \mathbf{vh}^{+} \mathbf{vh}^{-} \langle \mathbf{vh}^{+} \rangle$$

$$| \mathbf{vh}^{+} \mathbf{vh}^{-} \mathbf{vh}^{+} \mathbf{vh}^{-} \mathbf{$$

$$\varepsilon :: \mathbf{T}^{+} \operatorname{wh}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \mathbf{wh}^{+} \rangle$$

$$\varepsilon :: \mathbf{V}^{+} \mathbf{T}^{-} \langle \mathbf{V} \mathbf{wh}^{++} \rangle$$

$$| \mathbf{k} \mathbf{k} :: \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{k} \mathbf{k} :: \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{k} \mathbf{k} :: \mathbf{D}^{+} \mathbf{h}^{-} \quad \text{the } :: \mathbf{N}^{+} \mathbf{D}^{-} \langle \mathbf{N}^{+} \rangle$$

$$| \mathbf{k} \mathbf{k} \mathbf{k}^{+} \rangle \text{ teacher } :: \mathbf{P}^{+} \mathbf{N}^{-} \quad \text{father } :: \mathbf{P}^{+} \mathbf{N}^{-} \langle \mathbf{P}^{+} \rangle$$

$$| \mathbf{k} \mathbf{k}^{+} \rangle \text{ of } :: \mathbf{D}^{+} \mathbf{P}^{-} \quad \text{of } :: \mathbf{D}^{+} \mathbf{P}^{-} \langle \mathbf{D}^{+} \rangle$$

$$| \mathbf{k} \mathbf{k}^{+} \rangle = | \mathbf{k}^{-} \mathbf{k}^{+} \mathbf{k}^{+} \rangle$$

$$| \mathbf{k}^{+} \mathbf{k}^{+} \rangle = | \mathbf{k}^{-} \mathbf{k}^{+} \mathbf{k}^{+} \rangle$$

$$| \mathbf{k}^{+} \mathbf{k}^{+} \mathbf{k}^{+} \rangle = | \mathbf{k}^{+} \mathbf{k}^{+} | \mathbf{k}^{+} \mathbf{k}^{+} | \mathbf{k}^{+$$

### Restricting *move*



#### The Specifier Island Constraint (SpIC)

\*Who does a teacher of \_\_ like the father of John?

### Restricting *move*



#### The Specifier Island Constraint (SpIC)

1 \*Who does a teacher of \_\_ like the father of John?













### The SpIC guarantees STA recognition.

 $\varepsilon :: \mathbf{T}^+ \mathbf{wh}^+ \mathbf{C}^- \langle \mathbf{T}^+ \mathbf{wh}^+ \rangle$  $\varepsilon :: \stackrel{|}{\mathrm{V}^{+}} \mathrm{T}^{-} \left\langle \mathbf{V} \mathbf{w} \mathbf{h}^{++} \right\rangle$ like ::  $D^+ D^+ V^- \langle D^+ D^+ w h^+ \rangle$  $\left< \mathbf{P^+} \right> \ \text{teacher} :: \ \mathbf{P^+} \ \mathbf{N^-} \quad \text{father} :: \ \mathbf{P^+} \ \mathbf{N^-} \quad \left< \mathbf{P^+ w h^+} \right>$  $\left< \mathbf{D^+} \right> \text{ of } :: \begin{array}{c} | & \\ \mathbf{D^+} \ \mathbf{P^-} & \\ \cdot & \\ \end{array} \quad \text{ of } :: \begin{array}{c} | & \\ \mathbf{D^+} \ \mathbf{P^-} & \\ \left< \mathbf{D^+wh^+} \right> \end{array}$ John ::  $D^-$  who ::  $D^-$  wh<sup>-</sup>

### The SpIC guarantees STA recognition.

 $\varepsilon :: \mathbf{T}^+ \mathbf{wh}^+ \mathbf{C}^- \langle \mathbf{T}^+ \mathbf{wh}^+ \rangle$  $\varepsilon :: \stackrel{!}{\mathbf{V}^{+}} \mathbf{T}^{-} \left\langle \mathbf{V} \mathbf{w} \mathbf{h}^{++} \right\rangle$ like ::  $D^+ D^+ V^- \langle D^+ D^+ w h^+ \rangle$  $\left< \mathbf{P^+} \right> \ \text{teacher} :: \ \mathbf{P^+} \ \mathbf{N^-} \quad \text{father} :: \ \mathbf{P^+} \ \mathbf{N^-} \quad \left< \mathbf{P^+ w h^+} \right>$  $\left< \mathbf{D^+} \right> \text{ of } :: \begin{array}{c} | & \\ \mathbf{D^+} \ \mathbf{P^-} & \\ \mathbf{D^+} \ \mathbf{P^-} & \\ \mathbf{D^+} \ \mathbf{wh^+} \right>$  $\langle \varepsilon \rangle$  John :: D<sup>-</sup> who :: D<sup>-</sup> wh<sup>-</sup>  $\langle \varepsilon \rangle$ 









$$\varepsilon :: \mathbf{T}^{+} \mathbf{wh}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \mathbf{wh}^{+} \rangle$$

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$$| \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \rangle$$

$$| \mathbf{W}^{+} \mathbf{D}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \rangle$$

$$| \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \rangle$$

$$| \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \mathbf{W}^{+} \rangle$$

$$| \mathbf{W}^{+} \mathbf{W}$$

$$\varepsilon :: \mathbf{T}^{+} \mathbf{wh}^{+} \mathbf{C}^{-} \langle \mathbf{T}^{+} \mathbf{wh}^{+} \rangle$$

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$$| \mathbf{kes} :: \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

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$$| \mathbf{V}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{D}^{+} \mathbf{wh}^{+} \rangle$$

$$| \mathbf{V}^{+} \mathbf{V}^{-} \langle \mathbf{D}^{+} \mathbf{vh}^{+} \rangle$$

$$| \mathbf{V}^{+} \mathbf{V}^{-} \langle \mathbf{N}^{+} \mathbf{vh}^{+} \rangle$$

$$| \mathbf{V}^{+} \mathbf{V}^{-} \langle \mathbf{N}^{+} \mathbf{vh}^{+} \rangle$$

$$| \mathbf{V}^{+} \mathbf{vh}^{-} \mathbf{vh}^{+} \mathbf{vh}^{-} \langle \mathbf{vh}^{+} \rangle$$

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## Interim Summary [2]

### We are looking for a complexity upper bound for syntax...

### The road so far

- ► MDEP[merge]  $\subsetneq$  STA
- ► MDEP[merge,move]  $\nsubseteq$  STA
- ▶ But MDEP[merge,move] ⊊ STA if we restrict move Movement constraints follow naturally: SpIC, CSC, ...

But syntax is not just about core operations!

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#### But syntax is not just about core operations!

## Licensing Conditions

### Syntax is not just about Merge and Move...

#### NPI licensing

1a) \*Every student said that the train ever arrives on time.1b) No student said that the train ever arrives on time.

#### Principle A

2a) \*John said that Mary likes himself.2b) John said that Mary likes herself.

#### Graf and Shafiei (2019)

Licensing conditions are (sub)regular over c-command strings.

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Principle A

Reflexives must be bound within their binding domain (e.g. TP).

 $\varepsilon :: T^+ C^ \varepsilon :: V^+ T^$ said ::  $D^+ C^+ V^-$ John ::  $D^-$  that ::  $T^+ C^ \varepsilon :: \, \mathbf{V}^+ \ \mathbf{T}^$ likes ::  $D^+ D^+ V^$ herself ::  $D^{-}$ Mary ::  $D^-$ 

Principle A



Principle A



Principle A



Principle A



Principle A



Principle A



Principle A



Principle A



#### Principle A



#### Principle A



Principle A



#### Principle A



Principle A



Principle A



Principle A



Principle A



Principle A



### Conclusion

#### STA as an upper bound for syntax

- ► MDEP[merge,move] ⊊ STA if we restrict move
- STA and C-Command Conditions

#### Merge, Move, Licensing enforced by the same machinery!

- MDEP a natural encoding of head-argument relations
- Naturalness of c-command
- $\blacktriangleright$  STA-recognition  $\approx$  syntactically motivated restrictions
- interaction of movement and licensing is expected

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### Conclusion?

#### STA as a uniform upper bound. But:

- Too permissive: Enforce arbitrary regular constraints
- ► Too restrictive? Licensing + c-command...

#### **Expanding the Core Results**

- Movement + licensing
- Subcommand
- Adjunct Island Constraint, Coordinate Structure Constraint, ...
- MG derivation trees?
- Improving top-down parsing efficiency

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 $\langle Thank you! \rangle$ 

## Acknowledgments I



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### The Spine of a Node

Example: spine(a)



#### STAs and spine closure (Martens 2006)

A regular tree language L belongs to the class STA iff L is spine closed.

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# Spine Closure





## Subregular Complexity in Phonology

Subregular phonology has proved to be a fruitful enterprise (Heinz et al. 2011; Chandlee 2014; Jardine 2016; McMullin 2016; Graf 2017; Graf and Mayer 2018)

 KEG

 SF/DBSP

 LTT

 M-IOTSL

 LT

 MTSL

 IO-TSL

 ID



### Graf and Shafiei (2019)

C-command conditions as subregular c-string constraints.



Observation |

 $spine(u) \approx c-string(u)$ 

#### Theorem

Every regular c-string constraint can be enforced by an STA.

 $\mathsf{c}\operatorname{-string}(\mathsf{the}::\,\mathsf{N}^+\;\mathsf{D}^-):=\varepsilon::\,\mathsf{T}^+\;\mathsf{wh}^+\;\mathsf{C}^-\uparrow\operatorname{does}::\,\mathsf{V}^+\;\mathsf{T}^-\uparrow\operatorname{like}::\,\mathsf{D}^+\;\mathsf{D}^+\;\mathsf{V}^-\uparrow\mathsf{a}::\,\mathsf{N}^+\;\mathsf{D}^-\;\mathsf{the}::\,\mathsf{N}^+\;\mathsf{D}^-$ 

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# Merge is SL (Graf 2012)



#### SL constraints on Merge

- We lift constraints from string n-grams to tree n-grams
- We get SL constraints over subtrees.



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# Non-Local Dependencies in Syntax

- Let's stick to core operations:
  - Move
  - Merge: Unbounded adjunction
    - ??



# TSL over Trees: Projecting Tiers



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### A TSL grammar for Merge **1** Project Merge iff a child has $X^+$ (e.g. X = N)



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## Constraints on Move

#### What about Move?

Suppose our MG is in **single movement normal form**, i.e. every phrase moves at most once. Then movement is regulated by two constraints. (Graf 2012

#### Constraints on Movement

- Move Every head with a negative Move feature is dominated by a matching Move node.
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## Move Constraints over Tiers

#### Original

- **Move** Every head with a negative Move feature is dominated by a matching Move node.
- **SMC** Every Move node is a closest dominating match for exactly one head.

#### Tier

Every lexical item has a **mother** labeled Move.

Exactly one of a Move node's **daughters** is a lex-ical item.

Tree <i>n</i> -gram Templates				
	Move	SMC1	SMC2	
	\$	Move	Move	
-	$\geq 1 \text{ LI}$	no LI	$\geq 2$ Lls	