



# Computation as a Window into Linguistic Cognition

**Aniello De Santo**

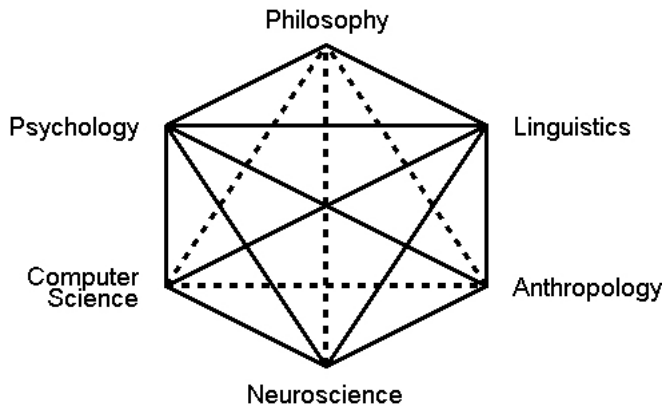
he/him

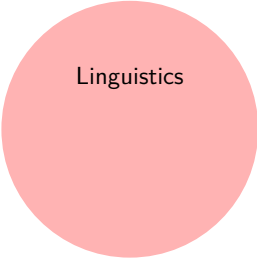
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University of Michigan, Ann Arbor  
February 2024

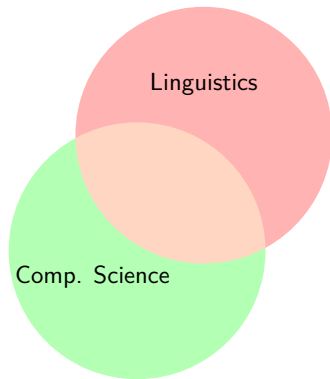
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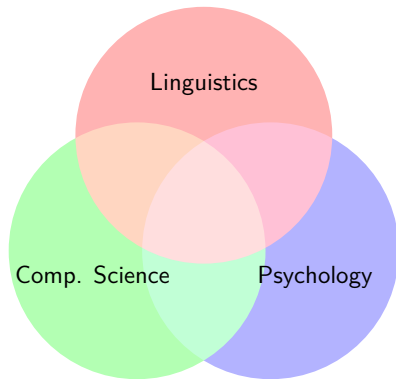


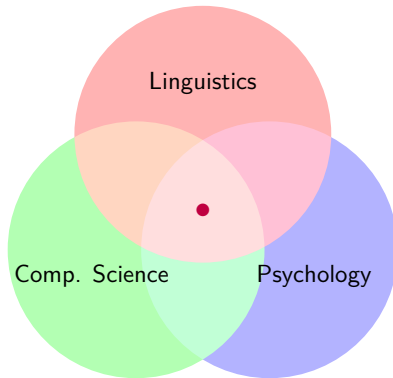


Linguistics

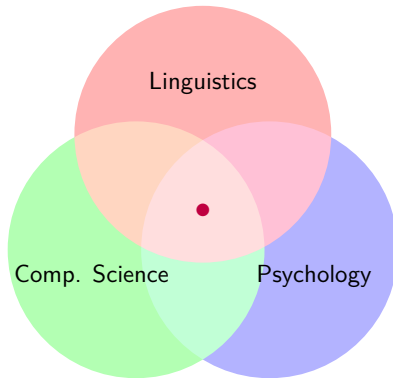






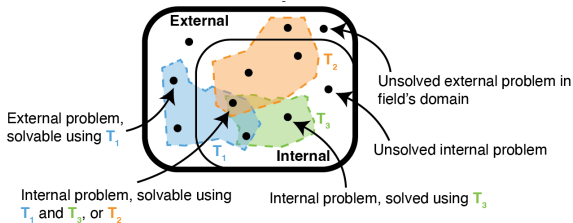


- ▶ **Theory building** (De Santo & Rawski 2022, Baggio, De Santo, Nunez 2024, Levenstein et al. 2024)
- ▶ **Computational invariants in typology and acquisition**  
(De Santo & Graf 2019, De Santo & Aksenova 2021, Johnson and De Santo 2023)
- ▶ **Computational parallels across linguistic modules**  
(Aksenova & De Santo 2017, Graf & De Santo 2020, De Santo 2018, Miller & De Santo 2023, a.o.)
- ▶ **Memory traces of processing generalized quantifiers** (De Santo et al. 2019, De Santo & Drury 2020)
- ▶ **Modeling processing difficulty** (De Santo 2019, 2021, 2022, a.o.)
- ▶ **Gradience in acceptability judgment** (De Santo 2020)
- ▶ **Evaluating/Contrasting syntactic analyses**  
(De Santo & Shafiei 2019, Lee & De Santo 2022, Del Valle & De Santo 2023, a.o.)
- ▶ **Locality and Economy Considerations** (De Santo & Lee 2022a)
- ▶ **Online/Offline effects in sentence processing**  
(De Santo & Lee 2022b, Lee & De Santo in prep., Jacobs, De Santo, Grobol in prep.)
- ▶ **Animal Cognition** (De Santo & Rawski, 2021)
- ▶ **Mapping syntactic and prosodic constituents** (Vu, De Santo, Dolatian 2022)
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- ▶ ...

# Problems and Theories<sup>1</sup>



## Some Problems

- ▶ what are the core representations?
- ▶ what do they tell us about processing?
- ▶ what do they tell us about learning?

<sup>1</sup>Levenstein, De Santo, ..., et al. (2024), Guest & Martin (2021), a.o.

# Computation and Theory Building

*[...] this is a confusion of two quite separate issues, **simulation and explanation**. [...] What we are **really** interested in [...] is explanation — in developing models that help us **understand how it is that people behave** that way, not merely demonstrating that we can build an artifact that behaves similarly.*

*(Kaplan, 1995)*

- ▶ Invariant properties of phenomena
- ▶ Specification of verbal theories

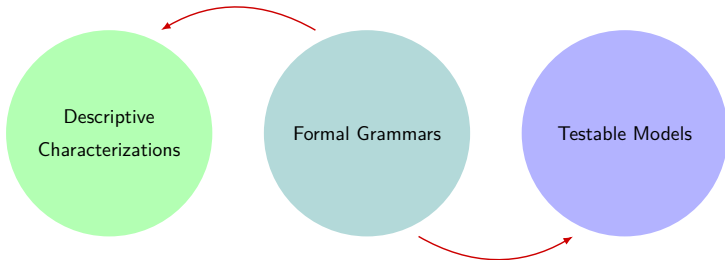
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# Building Bridges



# Outline

- 1 Theory Building
- 2 Linguistics and Formal Language Theory
- 3 MG Parsing as a Model of Gradience
- 4 Conclusion



# Theories from Data?

## Theories of linguistic representations from typological/empirical observations?

*The problem that we cannot deduce [...] theories from data is a limitation, or **perhaps an attribute**, of all empirical science [...] Still, one may abduce hypotheses [...] Abduction is **reasoning from observations** [...] It consists of two steps: generating candidate **hypotheses** (abduction proper), and selecting the “best” explanatory one[s] (inference to the **best explanation**).*

*(van Roji & Baggio 2020, pg. 9)*

# Theories from Data?

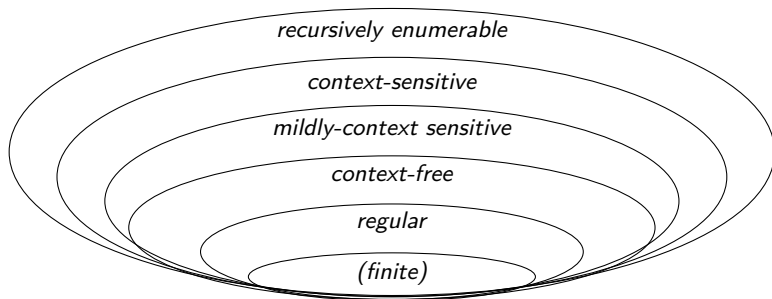
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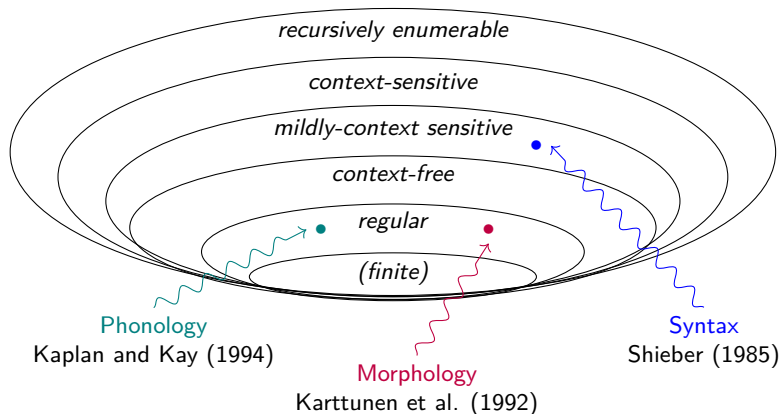
# A Lens: Computational Theories of Language

Stringsets can be classified according to the requirements of the grammars that generate them.

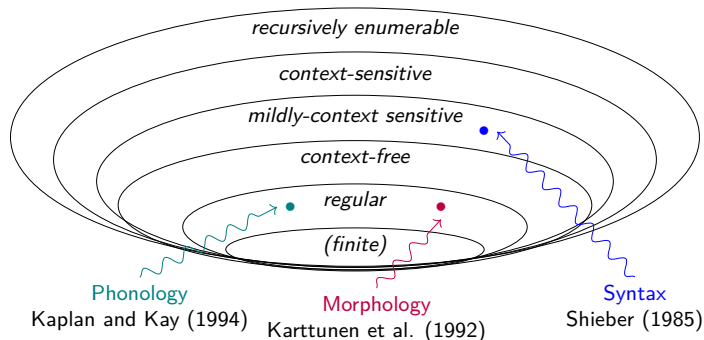


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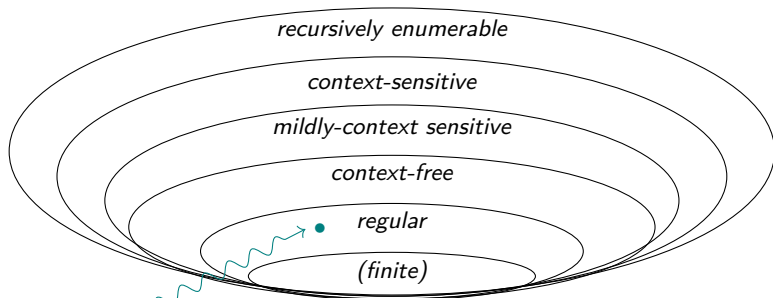
# Precise Characterizations $\Rightarrow$ Precise Predictions



## Precise predictions for:

- ▶ typology  $\rightarrow$  e.g. no center embedding in phonology
- ▶ learnability  $\rightarrow$  e.g. no Gold learning for regular languages
- ▶ cognition  $\rightarrow$  e.g. finitely bounded working memory

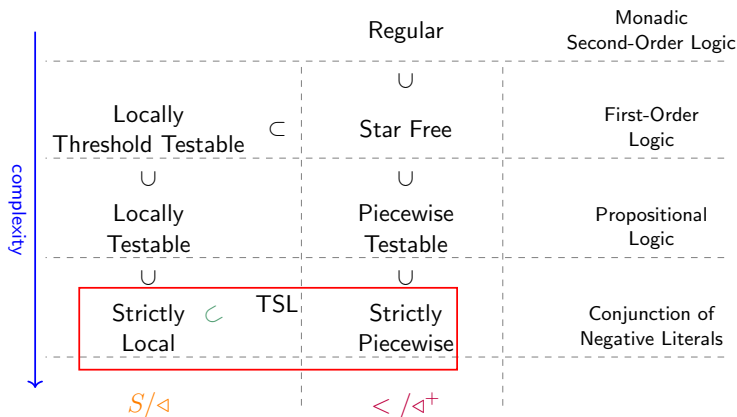
# Spoken Languages' Phonology as a Regular System



Phonology

Kaplan and Kay (1994)

# Beyond Monolithic Classes: Subregular Languages<sup>2</sup>



<sup>2</sup>McNaughton & Papert (1976), Heinz (2011), Chandlee & Heinz (2014), De Santo & Graf (2019), De Santo & Rawski (2022), a.o.

# Local Phonotactic Dependencies

## 1 Word-final devoicing

Forbid voiced segments at the end of a word

- (1) a. \*rad
- b. rat

## 1 Intervocalic voicing

Forbid voiceless segments in between two vowels

- (2) a. \*faser
- b. fazer

These patterns can be described by **strictly local** (SL) constraints.



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# Local Dependencies in Phonology are SL

## Example: Word-final devoicing

- ▶ Forbid voiced segments at the end of a word:  $*[+voice]\$$
- ▶ **German:**  $*z\$, *v\$, *d\$$  ( $\$$  = word edge).

\$ r a **d** \$                      \$ r a t \$

## Example: Intervocalic voicing

- ▶ Forbid voiceless segments in-between two vowels:  $*V[-voice]V$
- ▶ **German:**  $*ase, *ise, *ese, *isi, \dots$

\$ f a **s** e r \$                      \$ f a z e r \$

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## Example: Intervocalic voicing

- ▶ Forbid voiceless segments in-between two vowels:  $*V[-voice]V$
- ▶ **German:**  $*a\textcolor{red}{s}e, *i\textcolor{red}{s}e, *e\textcolor{red}{s}e, *i\textcolor{red}{s}i, \dots$

\\$   f   a   s   e   r   \\$

\\$   f   a   z   e   r   \\$

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# Unbounded Dependencies Are Not SL

## ► Samala Sibilant Harmony

Sibilants must not disagree in anteriority.

(Applegate 1972)

- (3) a. \* ha<sup>s</sup>xintilawa<sup>f</sup>  
b. \* ha<sup>f</sup>xintilawa<sup>s</sup>  
c. ha<sup>f</sup>xintilawa<sup>f</sup>

Example: Samala

\*\$ ha<sup>s</sup>xintilawa<sup>f</sup>\$

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► **But:** Sibilants can be arbitrarily far away from each other!

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\* \$<sup>s</sup>tajanowonwa<sup>f</sup>\$

# Locality Over Tiers

\*\$**s**t a j a n o w n w a **j**!\$

- ▶ Sibilants can be arbitrarily far away from each other!
- ▶ **Problem:** SL limited to locality domains of size  $n$ ;

## Tier-based Strictly Local (TSL) Grammars (Heinz et al. 2011)

- ▶ Projection of selected segments on a tier  $T$   
(Goldsmith 1976)
- ▶ Strictly local constraints over  $T$  determine wellformedness
- ▶ Unbounded dependencies are local over **tiers**

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- ▶ Let's revisit Samala Sibilant Harmony

- I.E.  $^*S_I, ^*S_3, ^*Z_I, ^*Z_3, ^*\int S, ^*3S, ^*\int Z, ^*3Z$

Diagram illustrating the state of memory locations `s` and `ok` after the first iteration of the loop:

- Location `s` (red) contains the string `shaxintilaw` (blue).
- Location `ok` (green) contains the string `shaxintilaw` (blue).

# Unbounded Dependencies are TSL

- ▶ Let's revisit Samala Sibilant Harmony


- (4) a. \* ha**s**xintilaw**ʃ**  
 b. \* ha**ʃ**xintilaw**s**  
 c. ha**ʃ**xintilaw**ʃ**

- ▶ What do we need to project? [+strident]
- ▶ What do we need to ban? \*[+ant][−ant], \*[−ant][+ant]


I.E. \***s**ʃ, \***s**ʒ, \***z**ʃ, \***z**ʒ, \*ʃ**s**, \*ʒ**s**, \*ʃ**z**, \*ʒ**z**

## Example: TSL Samala

\* \$ha**s**xintilaw**ʃ**\$



*ok* \$ha**ʃ**xintilaw**ʃ**\$



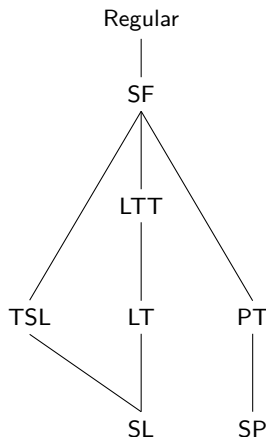
# SL and TSL: So What?

*Descriptive characterizations focus on the **nature of the information** [...] that is needed in order to distinguish [...] a pattern*

*Rogers & Pullum (2011)*

## Invariants (De Santo & Rawski 2022)

- ▶ SL: adjacency
- ▶ TSL: relativized adjacency



- ▶ **But** typological variation is complex...  
(McMullin 2016, Mayer & Major 2018, De Santo & Graf 2019)

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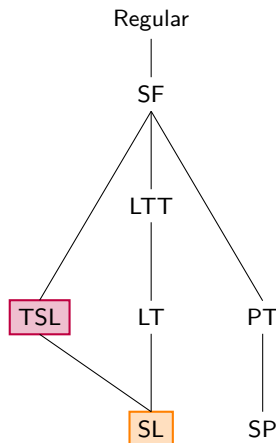
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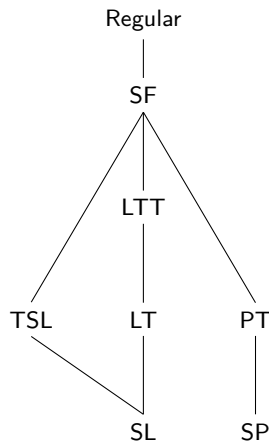




# Refining the Hierarchy via Typological Insights

## Observation

TSL is not closed under intersection  
(De Santo & Graf, 2019)



- ▶ We want to also account for multiple processes  
So we can cover the complete phonotactics of a language
- ▶ Multiple non-interacting processes in attested patterns

# Concurrent Processes

## Sibilant Harmony in IMDLAWN TASHLHIYT<sup>3</sup>

1) Underlying causative prefix /s(ɿ)-/

	<i>Base</i>	<i>Causative</i>	
--	-------------	------------------	--

a.	uga	sɿ-uga	"be evacuated"
----	-----	--------	----------------

b.	asɿ:twɑ	s-asɿ:twɑ	"settle, be levelled"
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<sup>3</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

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### 2) Sibilant harmony

	<i>Base</i>	<i>Causative</i>	
a.	fiaʃr	ʃ- fiaʃr	"be full of straw, of discord"
b.	nza	z:-nza	"be sold"

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### 3) Sibilant voicing harmony blocked

	<i>Base</i>	<i>Causative</i>	
a.	ukz	sɿ-ukz	"recognize"
b.	quɿi	ʃ- quɿi	"be dislocated, broken"

<sup>3</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

# Sibilant Harmony in IMDLAWN TASHLHIYT <sup>4</sup>

## Generalization (1/2)

Sibilants must agree in anteriority and voicing.

## Grammar

$$T = \{ \text{ʒ, s, z, ʃ} \}$$

$$S = \{ {}^*s\text{ʒ}, {}^*sz, {}^*sʃ, {}^*\text{ʒ}s, {}^*\text{ʃ}s, {}^*zs, {}^*zʃ, {}^*z\text{ʒ}, {}^*\text{ʃ}z, {}^*\text{ʃ}\text{ʒ}, {}^*\text{ʒ}\text{ʃ}, {}^*\text{ʒ}z \}$$

*\* z m: ʒ d a w l*

*ok ʒ m: ʒ d a w l*

<sup>4</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

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z      ʒ

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# Sibilant Harmony in IMDLAWN TASHLHIYT <sup>5</sup>

## Generalization (2/2)

Voiceless obstruents block agreement in voicing.

## Grammar

$$T = \{ \text{ʒ}, s, z, \text{ʃ}, q \}$$

$$S = \{ {}^*s\text{ʒ}, {}^*sz, {}^*s\text{ʃ}, {}^*\text{ʒ}s, {}^*\text{ʃ}s, {}^*zs, {}^*z\text{ʃ}, {}^*z\text{ʒ}, {}^*\text{ʃ}z, {}^*\text{ʃ}\text{ʒ}, {}^*\text{ʒ}\text{ʃ}, {}^*\text{ʒ}z \}$$

*ok*    ʃ    q    u    ʒ:    i

*\**    s    q    u    ʒ:    i

<sup>5</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

# Sibilant Harmony in IMDLAWN TASHLHIYT <sup>5</sup>

## Generalization (2/2)

Voiceless obstruents block agreement in voicing.

## Grammar

$$T = \{ \text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q} \}$$

$$S = \{ {}^*\text{sʒ}, {}^*\text{sz}, {}^*\text{sʃ}, {}^*\text{ʒs}, {}^*\text{ʃs}, {}^*\text{zs}, {}^*\text{zʃ}, {}^*\text{zʒ}, {}^*\text{ʃz}, {}^*\text{ʃʒ}, {}^*\text{ʒʃ}, {}^*\text{ʒz} \}$$

ʃ q ʒ:

.....

ok ʃ q u ʒ: i                      \* s q u ʒ: i

<sup>5</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

# Sibilant Harmony in IMDLAWN TASHLHIYT <sup>5</sup>

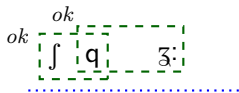
## Generalization (2/2)

Voiceless obstruents block agreement in voicing.

## Grammar

$$T = \{ \text{ʒ}, s, z, \text{ʃ}, q \}$$

$$S = \{ *s\text{ʒ}, *s\text{z}, *s\text{ʃ}, *\text{ʒ}s, *\text{ʃ}s, *zs, *z\text{ʃ}, *z\text{ʒ}, *\text{ʃ}z, *\text{ʃ}\text{ʒ}, * \text{ʒ}\text{ʃ}, *\text{ʒ}z \}$$



$ok$   $\text{ʃ}$   $q$   $u$   $\text{ʒ}:$   $i$

\*  $s$   $q$   $u$   $\text{ʒ}:$   $i$

<sup>5</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

# Sibilant Harmony in IMDLAWN TASHLHIYT <sup>5</sup>

## Generalization (2/2)

Voiceless obstruents block agreement in voicing.

## Grammar

$$T = \{ \text{ʒ}, s, z, \text{f}, q \}$$

$$S = \{ *s\text{ʒ}, *sz, *s\text{f}, *ʒs, *ʒs, *zs, *z\text{f}, *z\text{ʒ}, *fz, *f\text{ʒ}, * \text{ʒf}, *ʒz \}$$

*ok*

*ʃ* *q* *ʒ:*

.....

*ok*

*ʃ* *q* *u* *ʒ:* *i*

*s* *q* *ʒ:*

.....

\* *s* *q* *u* *ʒ:* *i*

<sup>5</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

# Sibilant Harmony in IMDLAWN TASHLHIYT <sup>5</sup>

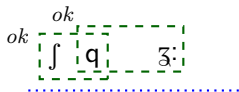
## Generalization (2/2)

Voiceless obstruents block agreement in voicing.

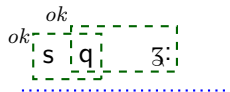
## Grammar

$$T = \{ \text{ʒ}, s, z, \text{f}, q \}$$

$$S = \{ *s\text{ʒ}, *sz, *s\text{f}, *\text{ʒ}s, *\text{f}s, *zs, *z\text{f}, *z\text{ʒ}, *\text{f}z, *\text{f}\text{ʒ}, *\text{ʒ}\text{f}, *\text{ʒ}z \}$$



$\text{ʒ} \text{ q } u \text{ ʒ} : i$



$* s \text{ q } u \text{ ʒ} : i$

<sup>5</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

# Sibilant Harmony in IMDLAWN TASHLHIYT <sup>5</sup>

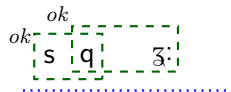
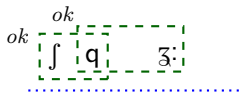
## Generalization (2/2)

Voiceless obstruents block agreement in voicing.

## Grammar

$$T = \{ \text{ʒ}, s, z, \text{ʃ}, q \}$$

$$S = \{ *s\text{ʒ}, *sz, *s\text{ʃ}, *\text{ʒ}s, *\text{ʃ}s, *zs, *z\text{ʃ}, *z\text{ʒ}, *\text{ʃ}z, *\text{ʃ}\text{ʒ}, *\text{ʒ}\text{ʃ}, *\text{ʒ}z \}$$



ok ʃ q u ʒ: i

\* s q u ʒ: i

<sup>5</sup> Elmedlaoui (1995), Hansson (2010), McMullin (2016), De Santo (2018)

# Multi-Tier Strictly Local (MTSL) Languages (1/2)<sup>6</sup>

## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, s, z, \text{ʃ}, q\} \quad S_1 = \{^*s\text{ʒ}, ^*sz, ^*\text{ʒ}s, ^*zs, ^*\text{ʃ}z, ^*\text{ʃ}\text{ʒ}, ^*\text{ʒ}\text{ʃ}\}$$

*ok*    ʃ    q    u    ʒ:    i

---

<sup>6</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

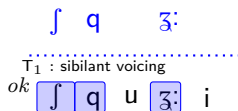


# Multi-Tier Strictly Local (MTSL) Languages (1/2)<sup>6</sup>

## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q}\} \quad S_1 = \{*\text{sʒ}, *\text{sz}, *\text{ʒs}, *\text{zs}, *\text{ʃz}, *\text{ʒʃ}, *\text{ʒʃ}\}$$



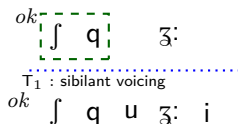
<sup>6</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (1/2)<sup>6</sup>

## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q}\} \quad S_1 = \{*\text{sʒ}, *\text{sz}, *\text{ʒs}, *\text{zs}, *\text{ʃz}, *\text{ʒʃ}, *\text{ʒʃ}\}$$



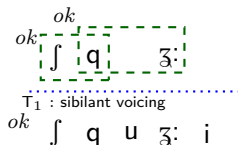
<sup>6</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (1/2)<sup>6</sup>

## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q}\} \quad S_1 = \{*\text{sʒ}, *\text{sz}, *\text{ʒs}, *\text{zs}, *\text{ʃz}, *\text{ʒʃ}, *\text{ʒʃ}\}$$



<sup>6</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (1/2)<sup>6</sup>

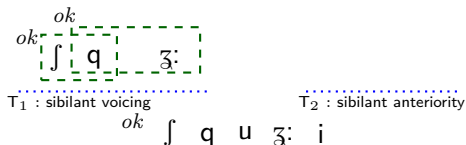
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q}\} \quad S_1 = \{^*\text{sʒ}, ^*\text{sz}, ^*\text{ʒs}, ^*\text{zs}, ^*\text{ʃz}, ^*\text{ʒʃ}, ^*\text{ʒʃ}\}$$

Unbounded agreement in anteriority:

$$\blacktriangleright T_2 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}\} \quad S_2 = \{^*\text{sʒ}, ^*\text{sʃ}, ^*\text{ʒs}, ^*\text{ʃs}, ^*\text{zs}, ^*\text{zʃ}, ^*\text{zʒ}, ^*\text{ʒz}, ^*\text{ʒz}\}$$



<sup>6</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (1/2)<sup>6</sup>

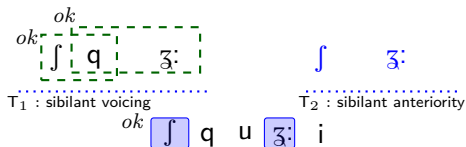
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q}\} \quad S_1 = \{*\text{sʒ}, *\text{sz}, *\text{ʒs}, *\text{zs}, *\text{ʃz}, *\text{ʃʒ}, *\text{ʒʃ}\}$$

Unbounded agreement in anteriority:

$$\blacktriangleright T_2 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}\} \quad S_2 = \{*\text{sʒ}, *\text{sʃ}, *\text{ʒs}, *\text{ʃs}, *\text{zs}, *\text{zʃ}, *\text{zʒ}, *\text{ʃz}, *\text{ʒz}\}$$



<sup>6</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (1/2)<sup>6</sup>

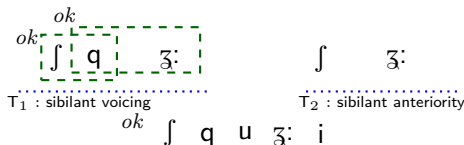
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q}\} \quad S_1 = \{*\text{sʒ}, *\text{sz}, *\text{ʒs}, *\text{zs}, *\text{ʃz}, *\text{ʃʒ}, *\text{ʒʃ}\}$$

Unbounded agreement in anteriority:

$$\blacktriangleright T_2 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}\} \quad S_2 = \{*\text{sʒ}, *\text{sʃ}, *\text{ʒs}, *\text{ʃs}, *\text{zs}, *\text{zʃ}, *\text{zʒ}, *\text{ʃz}, *\text{ʒz}\}$$



<sup>6</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (1/2)<sup>6</sup>

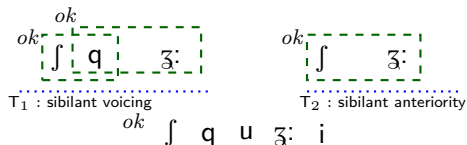
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q}\} \quad S_1 = \{*\text{sʒ}, *\text{sz}, *\text{ʒs}, *\text{zs}, *\text{ʃz}, *\text{ʃʒ}, *\text{ʒʃ}\}$$

Unbounded agreement in anteriority:

$$\blacktriangleright T_2 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}\} \quad S_2 = \{*\text{sʒ}, *\text{sʃ}, *\text{ʒs}, *\text{ʃs}, *\text{zs}, *\text{zʃ}, *\text{zʒ}, *\text{ʃz}, *\text{ʒz}\}$$



<sup>6</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (2/2)<sup>7</sup>

## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, s, z, \text{ʃ}, q\} \quad S_1 = \{^*s\text{ʒ}, ^*sz, ^*\text{ʒ}s, ^*zs, ^*\text{ʃ}z, ^*\text{ʃ}\text{ʒ}, ^*\text{ʒ}\text{ʃ}\}$$

Unbounded agreement in anteriority:

$$\blacktriangleright T_2 = \{\text{ʒ}, s, z, \text{ʃ}\} \quad S_2 = \{^*s\text{ʒ}, ^*s\text{ʃ}, ^*\text{ʒ}s, ^*\text{ʃ}s, ^*zs, ^*z\text{ʃ}, ^*\text{ʒ}z, ^*\text{ʃ}z, ^*\text{ʒ}z\}$$

\* s q u ʒ: i

<sup>7</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)



# Multi-Tier Strictly Local (MTSL) Languages (2/2)<sup>7</sup>

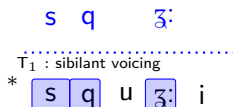
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, s, z, \text{ʃ}, q\} \quad S_1 = \{^*s\text{ʒ}, ^*sz, ^*\text{ʒ}s, ^*zs, ^*\text{ʃ}z, ^*\text{ʒ}\text{ʃ}, ^*\text{ʒ}\text{ʃ}\}$$

Unbounded agreement in anteriority:

$$\blacktriangleright T_2 = \{\text{ʒ}, s, z, \text{ʃ}\} \quad S_2 = \{^*s\text{ʒ}, ^*s\text{ʃ}, ^*\text{ʒ}s, ^*\text{ʃ}s, ^*zs, ^*z\text{ʃ}, ^*z\text{ʒ}, ^*\text{ʃ}z, ^*\text{ʒ}z\}$$



<sup>7</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (2/2)<sup>7</sup>

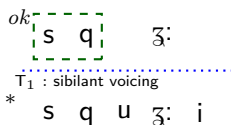
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, s, z, \text{ʃ}, q\} \quad S_1 = \{^*s\text{ʒ}, ^*sz, ^*\text{ʒ}s, ^*zs, ^*\text{ʃ}z, ^*\text{ʒ}\text{ʃ}, ^*\text{ʒ}\text{ʃ}\}$$

Unbounded agreement in anteriority:

$$\blacktriangleright T_2 = \{\text{ʒ}, s, z, \text{ʃ}\} \quad S_2 = \{^*s\text{ʒ}, ^*s\text{ʃ}, ^*\text{ʒ}s, ^*\text{ʃ}s, ^*zs, ^*z\text{ʃ}, ^*\text{ʒ}z, ^*\text{ʃ}z, ^*\text{ʒ}z\}$$



<sup>7</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (2/2)<sup>7</sup>

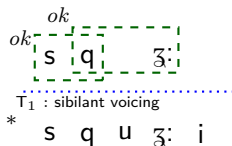
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, s, z, \text{ʃ}, q\} \quad S_1 = \{^*s\text{ʒ}, ^*sz, ^*\text{ʒ}s, ^*zs, ^*\text{ʃ}z, ^*\text{ʒ}\text{ʒ}, ^*\text{ʒ}\text{ʃ}\}$$

Unbounded agreement in anteriority:

$$\blacktriangleright T_2 = \{\text{ʒ}, s, z, \text{ʃ}\} \quad S_2 = \{^*s\text{ʒ}, ^*s\text{ʃ}, ^*\text{ʒ}s, ^*\text{ʃ}s, ^*zs, ^*z\text{ʃ}, ^*z\text{ʒ}, ^*\text{ʃ}z, ^*\text{ʒ}z\}$$



<sup>7</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (2/2)<sup>7</sup>

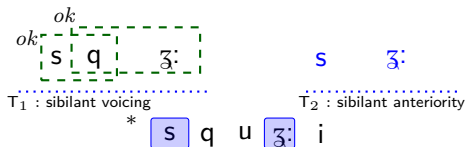
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

- $T_1 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}, \text{q}\}$   $S_1 = \{*\text{sʒ}, *\text{sz}, *\text{ʒs}, *\text{zs}, *\text{ʃz}, *\text{ʃʒ}, *\text{ʒʃ}\}$

Unbounded agreement in anteriority:

- $T_2 = \{\text{ʒ}, \text{s}, \text{z}, \text{ʃ}\}$   $S_2 = \{*\text{sʒ}, *\text{sʃ}, *\text{ʒs}, *\text{ʃs}, *\text{zs}, *\text{zʃ}, *\text{zʒ}, *\text{ʃz}, *\text{ʒz}\}$



<sup>7</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

# Multi-Tier Strictly Local (MTSL) Languages (2/2)<sup>7</sup>

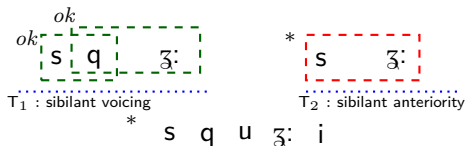
## Sibilant Harmony in IMDLAWN TASHLHIYT (Revisited)

Voiceless obstruents block agreement in voicing:

$$\blacktriangleright T_1 = \{\text{ʒ}, s, z, \text{ʃ}, q\} \quad S_1 = \{^*s\text{ʒ}, ^*sz, ^*\text{ʒ}s, ^*\text{ʒ}z, ^*\text{ʃ}z, ^*\text{ʃ}\text{ʒ}, ^*\text{ʒ}\text{ʃ}\}$$

Unbounded agreement in anteriority:

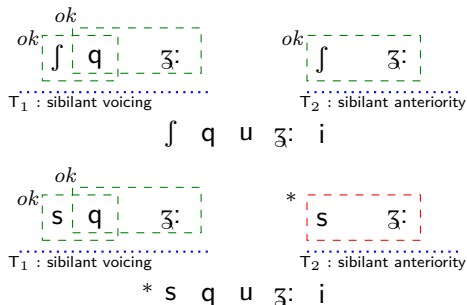
$$\blacktriangleright T_2 = \{\text{ʒ}, s, z, \text{ʃ}\} \quad S_2 = \{^*s\text{ʒ}, ^*s\text{ʃ}, ^*\text{ʒ}s, ^*\text{ʃ}s, ^*\text{ʒ}z, ^*z\text{ʃ}, ^*z\text{ʒ}, ^*\text{ʃ}z, ^*\text{ʒ}z\}$$



<sup>7</sup>McMullin (2016), De Santo (2018), De Santo & Graf (2019)

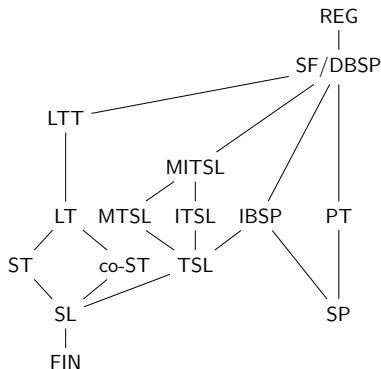
# Accounting for Concurrent Processes

- MTSL: TSL closure under intersection  
(De Santo & Graf, 2019)



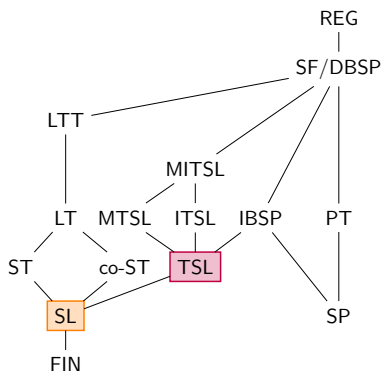
- Intersection closure accounts for multiple concurrent processes
- Can characterize the complete phonotactics of a language

# A Plethora of Combination (De Santo & Graf 2019)



- ▶ The goal is **not** identifying a single “correct” class
- ▶ Pinpoint fundamental properties of the patterns:  
SL:  $\triangleleft$  , TSL:  $\triangleleft_T$  , ...

# A Plethora of Combination (De Santo & Graf 2019)



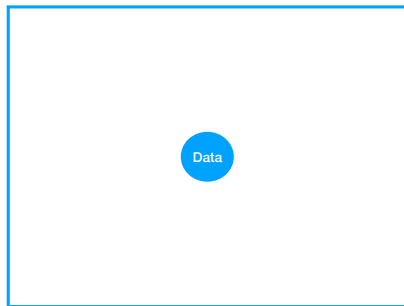
- ▶ The goal is **not** identifying a single “correct” class
- ▶ Pinpoint fundamental properties of the patterns:  
SL:  $\triangleleft$  , TSL:  $\triangleleft_T$  , ...
- ▶ What about learnability?



# Learning Multiple TSL Grammars<sup>8</sup>

## Problem:

- Unrestricted Hypothesis Spaces



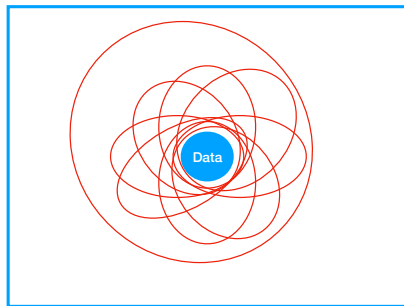
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<sup>8</sup>McMullin, Aksenova, De Santo (2020), De Santo & Aksenova (2021)

# Learning Multiple TSL Grammars<sup>9</sup>

## Problem:

- Unrestricted Hypothesis Spaces



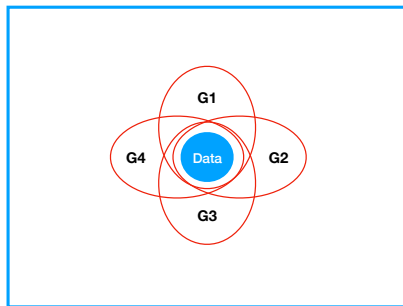
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<sup>9</sup>McMullin, Aksenova, De Santo (2020), De Santo & Aksenova (2021)

# Learning Multiple TSL Grammars<sup>10</sup>

## Solution:

- Structural priors



De Santo & Aksenova (2021):

⇒ Assume relativized locality!

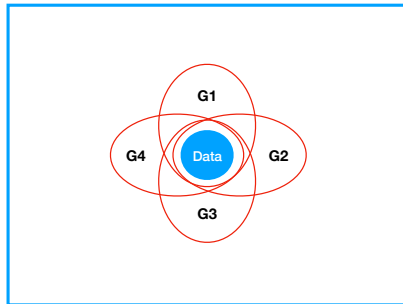
- tiers (but not their content)
- local tier constraints
- characteristic sample!

<sup>10</sup>McMullin, Aksenova, De Santo (2020), De Santo & Aksenova (2021)

# Learning Multiple TSL Grammars<sup>10</sup>

## Solution:

- Structural priors



De Santo & Aksenova (2021):

⇒ Assume relativized locality!

- tiers (but not their content)
- local tier constraints
- **characteristic sample!**

## Results

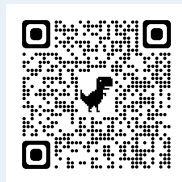
- No a priori information on the content of tiers/constraints
- Guaranteed convergence in polynomial time and data

<sup>10</sup>McMullin, Aksenova, De Santo (2020), De Santo & Aksenova (2021)

# Evaluating Convergence in Real World Scenarios

	SP	SL	TSL	MTSL	MITSL
Word-final devoicing					
T	✗	✓	✓	✓	✓
A	68%	100%	100%	100%	100%
N <sub>1</sub>	58%	100%	100%	100%	100%
Single vowel harmony without blocking					
T	✓	✗	✓	✓	✓
A	100%	83%	100%	100%	100%
N <sub>2</sub>	100%	72%	100%	100%	100%
Single vowel harmony with blocking					
T	✗	✗	✓	✓	✓
A	84%	89%	100%	100%	99%
Several vowel harmonies without blocking					
T	✓	✗	✓	✓	✓
A	100%	69%	100%	100%	100%
Several vowel harmonies with blocking					
T	✗	✗	✓	✓	✓
A	76%	59%	100%	100%	99%
N <sub>3</sub>	76%	70%	67%	95%	99%
Vowel harmony and consonant harmony without blocking					
T	✓	✗	✗	✓	✓
A	100%	64%	74%	100%	100%
Vowel harmony and consonant harmony with blocking					
T	✗	✗	✗	✓	✓
A	83%	64%	69%	100%	100%
Unbounded tone plateauing					
T	✓	✗	✗	✗	✓
A	100%	85%	90%		100%
Two locally-driven long-distance assimilations (ITSL restrictions)					
T	✗	✗	✗	✗	✓
A					100%

Johnson & De Santo (2023)



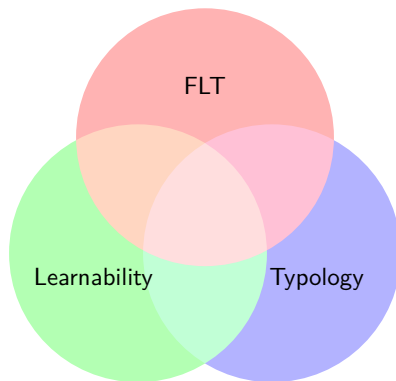
(T)heoretical expectations and performance of 5 subregular learners on (A)rtificial and simplified (N)atural language input data-sets. N<sub>1</sub>: German; N<sub>1</sub>: Finnish; N<sub>1</sub>: Turkish.

# Interim Summary

## SL and TSL for Spoken Phonotactics

- ▶ Linguistically natural (Goldsmith 1976)
- ▶ Captures (properties of a) wide range of (spoken) phonotactic dependencies (McMullin 2016, De Santo & Graf 2019)  
What about sign? (Rawski 2017, Rawski forth.)
- ▶ Provably correct and efficient learning algorithms  
(De Santo & Aksenova 2021, Johnson & De Santo u.r.)
- ▶ Predictions for human learning  
(Lai 2015, Avcu & Hestevic 2021, De Santo & Gutierrez in prep.)
- ▶ Generalizes beyond phonotactics  
(Aksenova & De Santo 2017, Graf & De Santo 2019, a.o.)

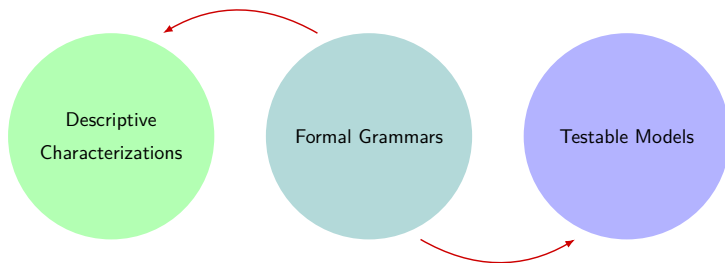
# Interim Summary [cont.]



## The Tip of the Iceberg:

- ▶ Cross-linguistic/cross-domain typological analysis
- ▶ Artificial language learning experiments
- ▶ New algorithms
- ▶ New mathematical insights

# Building Bridges





# Outline

- 1 Theory Building
- 2 Linguistics and Formal Language Theory
- 3 MG Parsing as a Model of Gradience**
- 4 Conclusion

# Acceptability and Grammaticality

- 1 What do you think that John bought *t*?
- 2 \*What do you wonder whether John bought *t*?

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*(Chomsky 1957)*

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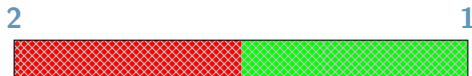
*One way to test the **adequacy of a grammar** proposed for [language] *L* is to determine whether or not the sequences that it generates are actually grammatical, i.e., **acceptable** [...]*

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Acceptability judgments  $\approx$  Grammaticality judgments

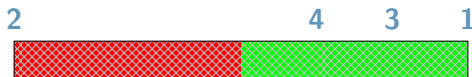
# Gradience in Acceptability Judgments

- 1 What do you think that John bought *t*?
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# Gradience in Acceptability Judgments

- 1 What do you think that John bought *t*?
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# Gradient Acceptability and Categorical Grammars

Acceptability judgments are not binary but *gradient*:

*An adequate linguistic theory will have to recognize **degrees of grammaticality** [...] there is little doubt that speakers can fairly consistently order new utterances, never previously heard, with respect to their **degree of belongingness to the language**.*

*(Chomsky 1975: 131-132)*



# (Quantitative) Models of Gradience

## Gradient Grammars (Keller 2000; Lau et al. 2014)

- ▶ OT-style constraint ranking
- ▶ Probabilistic grammars

## Extra-grammatical Factors (Chomsky 1975; Schütze 1996)

- ▶ Processing effects
  - ▶ Plausibility
  - ▶ Working memory limitations
  - ▶ **But:** few models for quantitative predictions!

## Building Linking Hypothesis

We need to link categorical grammars, processing difficulty, and gradience **explicitly**!

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# Forward to the Past

- ▶ What is the relation between grammatical operations and cognitive processes?

## Derivational Theory of Complexity (Miller and Chomsky, 1963)

- ▶ Processing complexity  $\sim$  length of a derivation  
(Fodor & Garrett 1967; Berwick & Weinberg 1983)
  - ▶ Essentially: there is a **cost** to mental computations.
- 
- ▶ What is the right notion of syntactic derivation?
  - ▶ What is costly? And why?

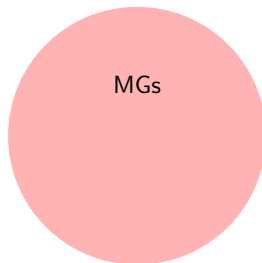
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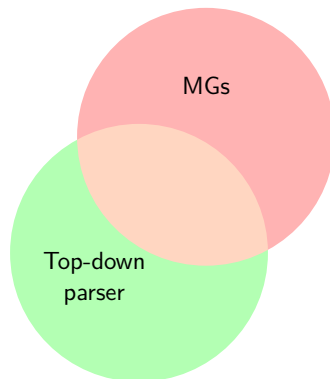
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# A Formal Model of Sentence Processing



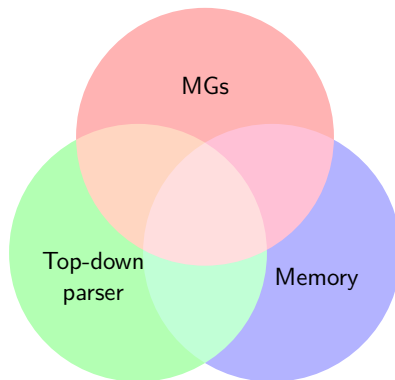
- 1 An explicit syntactic theory → Minimalist grammars (MGs)

# A Formal Model of Sentence Processing



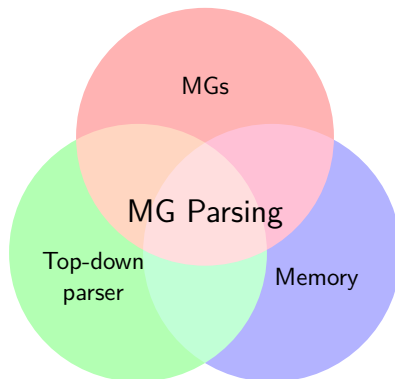
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# A Formal Model of Sentence Processing



- 1 An explicit syntactic theory → Minimalist grammars (MGs)
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# A Formal Model of Sentence Processing

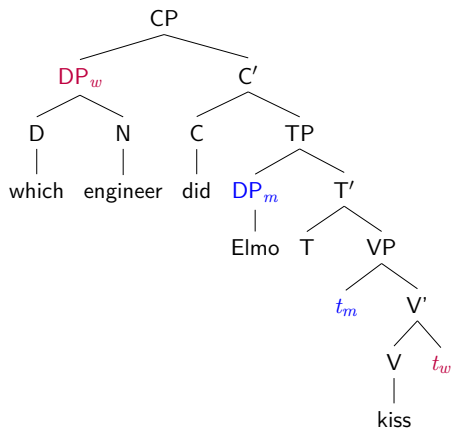


- 1 An explicit syntactic theory → Minimalist grammars (MGs)
- 2 A theory of how structures are built → Top-down parser
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**Interpretability for the win!**

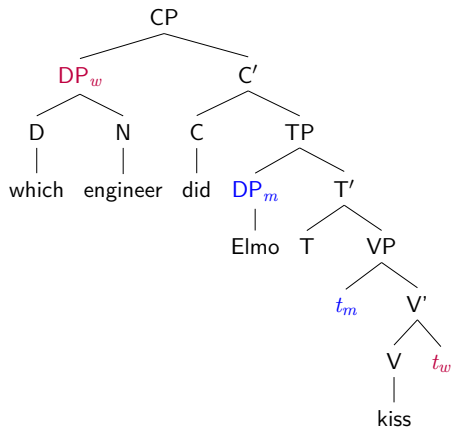


# Minimalist Grammars (MGs) & Derivation Trees

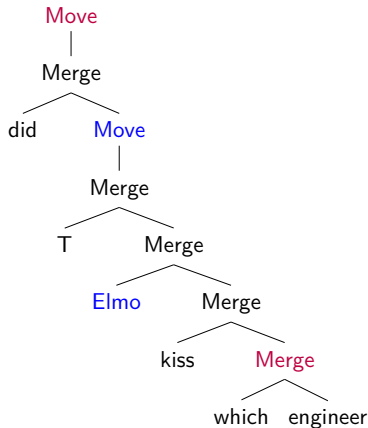


## Phrase Structure Tree

# Minimalist Grammars (MGs) & Derivation Trees

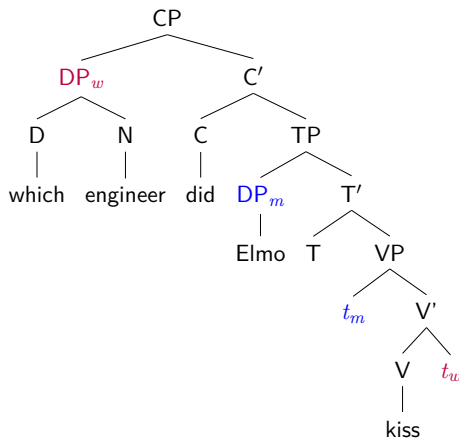


**Phrase Structure Tree**

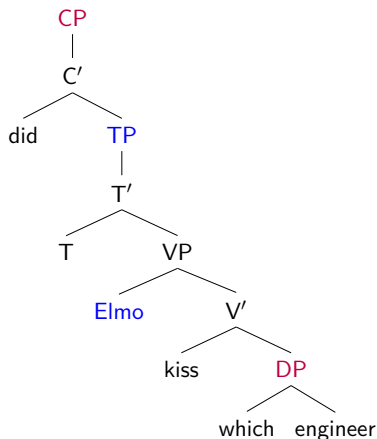


**Derivation Tree**

# MG Syntax: Derivation Trees

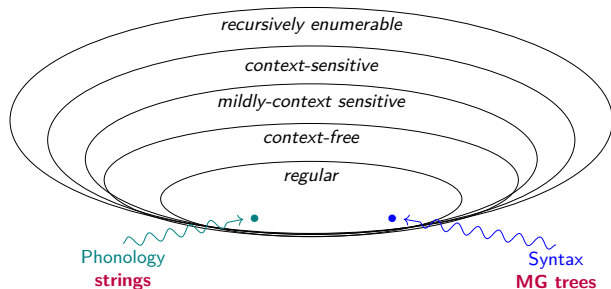
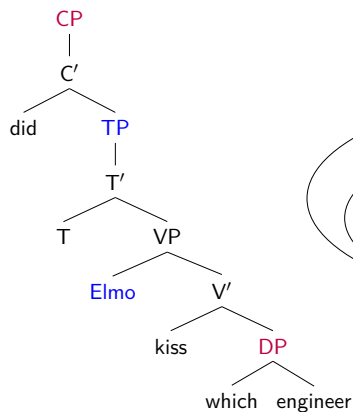


**Phrase Structure Tree**



**Derivation Tree**

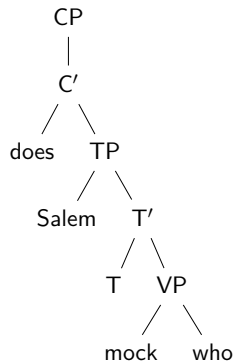
# Regular Tree Languages<sup>11</sup>



<sup>11</sup>Thatcher (1967), Koble et al. (2007), Stabler (2013)

# The Job of a Parser

Who does Salem mock?

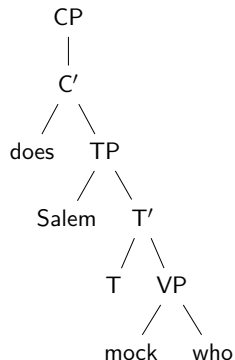


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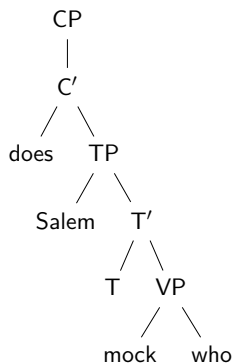
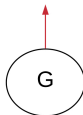


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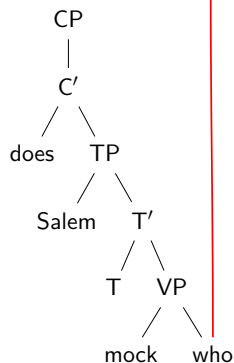
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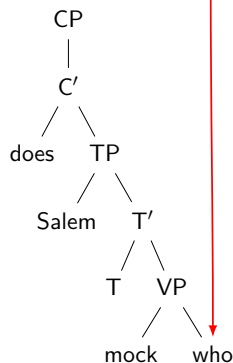


► Bottom-up



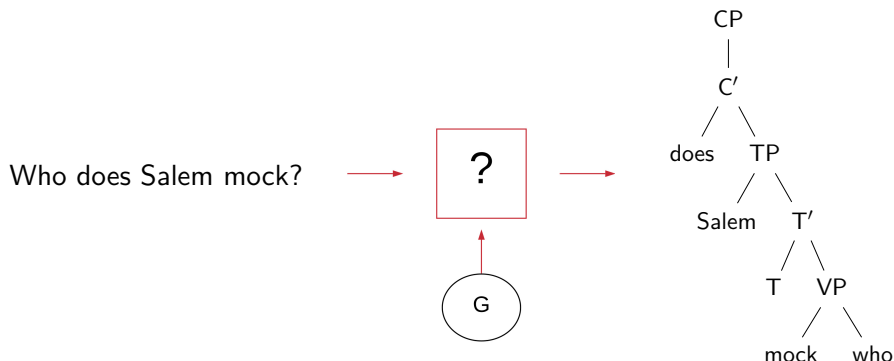
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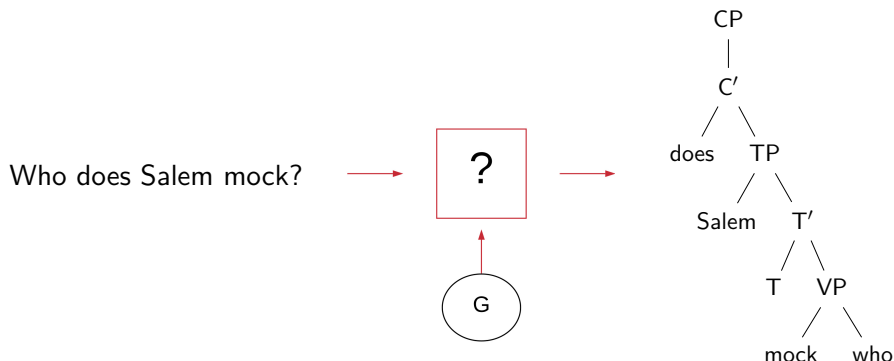
- ▶ Bottom-up
- ▶ Top-down

# The Job of a Parser



- ▶ Bottom-up
- ▶ **Top-down** (Stabler, 2013)
  - ▶ Psychologically plausible(-ish)

# The Job of a Parser



- ▶ Bottom-up
- ▶ **Top-down** (Stabler, 2013)
  - ▶ Psychologically plausible(-ish)
  - ▶ Assumption: Parser as an oracle!

# Incremental Top-Down Parsing: The Intuition

Who does Salem mock?

# Incremental Top-Down Parsing: The Intuition

CP

Who does Salem mock?

- ▶ Builds the structure from top to bottom
- ▶ Takes elements in an out of memory
- ▶ Complexity of the structure  $\approx$  how much memory is used!

# Incremental Top-Down Parsing: The Intuition

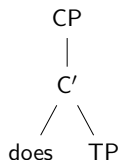
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|  
C'

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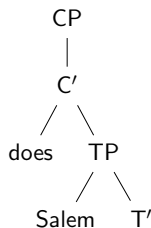
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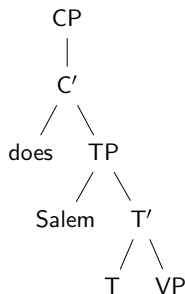


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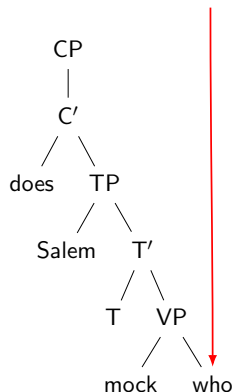
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Who does Salem mock?



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# Memory-Based Complexity Metrics

- ▶ **Memory usage:**

(Kobele et al. 2012; Gibson, 1998)

**Tenure** How long a node is kept in memory

**Size** How much information is stored in a node

⇒ Intuitively, the length of its movement dependency!

- ▶ Formalized into offline **complexity metrics**

MaxTenure  $\max(\{\text{tenure-of}(n) \mid n \text{ a node of the tree}\})$

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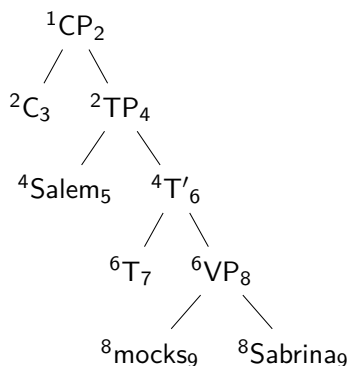
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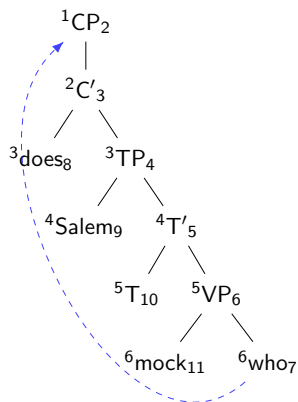
**MaxTenure**  $\max(\{\text{tenure-of}(n) \mid n \text{ a node of the tree}\})$

# Contrasting Derivations

**MaxTenure = 2**



**MaxTenure = 5**



# Summary of the Approach

A Computational Linking Hypothesis (De Santo 2020; in prep.)

Grammar  $\Leftrightarrow$  MG Parser Effort  $\Leftrightarrow$  Gradience

## General Idea

(Kobele et al. 2012; Gerth 2015; Graf et al. 2017; De Santo 2020)

- 1 Pick two competing derivations
- 2 Evaluate metrics over each
  - ▶ Lowest score means easiest!
- 3 Compare parser's prediction to experimental data



## A Proof of Concept: Back to Island Effects

- 1 What do you think that John bought *t*?
- 2 What do you wonder whether John bought *t*?
- 3 Who *t* thinks that John bought a car?
- 4 Who *t* wonders whether John bought a car?

Results in pairwise comparisons ideal for the MG parser

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## Gradience in Islands: Sprouse et al. (2012)

A factorial design for islands effects:

- 1 GAP POSITION: Matrix vs. Embedded
- 2 STRUCTURE: Island vs. Non-Island  
(Kluender & Kutas 1993)

Results in pairwise comparisons ideal for the MG parser



# A Proof of Concept: Back to Island Effects

- |   |   |                       |
|---|---|-----------------------|
| 1 | What do you think that John bought <i>t</i> ?     | Non-Island   Embedded |
| 2 | What do you wonder whether John bought <i>t</i> ? | Island   Embedded     |
| 3 | Who <i>t</i> thinks that John bought a car?       | Non-Island   Matrix   |
| 4 | Who <i>t</i> wonders whether John bought a car?   | Island   Matrix       |

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|---|---|-----------------------|
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Results in pairwise comparisons ideal for the MG parser

# Sprouse et al. (2012)

## ISLAND TYPES

### Subject islands

- ▶ **What** do you think the speech about *t* interrupted the show about global warming?

### Adjunct islands

- ▶ **What** do you laugh if John leaves *t* at the office?

### Complex NP islands

- ▶ **What** did you make the claim that John bought *t*?

## GAP POSITION × STRUCTURE

- 1 Matrix vs. Embedded
- 2 Island vs. Non-Island

# Modeling Results (De Santo 2020)

Island Type	Sprouse et al. (2012)			MG Parser	
Subj. Island 1	Subj.	Non Isl.	>	Obj.	Non Isl. ✓
	Subj.	Non Isl.	>	Obj.	Isl. ✓
	Subj.	Non Isl.	>	Subj.	Isl. ✓
	Obj.	Non Isl.	>	Obj.	Isl. ✓
	Obj.	Non Isl.	>	Subj.	Isl. ✓
	Obj.	Isl.	>	Subj.	Isl. ✗
Subj. Island 2	Matrix	Non Isl.	>	Emb.	Non Isl. ✓
	Matrix	Non Isl.	>	Matrix	Isl. ✓
	Matrix	Non Isl.	>	Emb.	Isl. ✓
	Matrix	Isl.	>	Emb.	Isl. ✓
	Matrix	Isl.	>	Matrix	Isl. ✓
	Emb.	Non Isl.	>	Emb.	Isl. ✓
Adj. Island	Matrix	Non Isl.	>	Emb.	Non Isl. ✓
	Matrix	Non Isl.	>	Matrix	Isl. ✓
	Matrix	Non Isl.	>	Emb.	Isl. ✓
	Matrix	Isl.	>	Emb.	Isl. ✓
	Matrix	Isl.	>	Matrix	Isl. ✓
	Emb.	Non Isl.	>	Emb.	Isl. ✓
CNP Island	Matrix	Non Isl.	>	Emb.	Non Isl. ✓
	Matrix	Non Isl.	=	Matrix	Isl. ✓
	Matrix	Non Isl.	>	Emb.	Isl. ✓
	Matrix	Isl.	>	Emb.	Isl. ✓
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	Subj.   Non Isl.	>	Subj.   Isl.		✓	
	Obj.   Non Isl.	>	Obj.   Isl.		✓	
	Obj.   Non Isl.	>	Subj.   Isl.		✓	
	<b>Obj.   Isl.</b>	<b>&gt;</b>	<b>Subj.   Isl.</b>		✗	
Subj. Island 2	Matrix   Non Isl.	>	Emb.   Non Isl.		✓	
	Matrix   Non Isl.	>	Matrix   Isl.		✓	
	Matrix   Non Isl.	>	Emb.   Isl.		✓	
	Matrix   Isl.	>	Emb.   Isl.		✓	
	Matrix   Isl.	>	Matrix   Isl.		✓	
	Emb.   Non Isl.	>	Emb.   Isl.		✓	
Adj. Island	Matrix   Non Isl.	>	Emb.   Non Isl.		✓	
	Matrix   Non Isl.	>	Matrix   Isl.		✓	
	Matrix   Non Isl.	>	Emb.   Isl.		✓	
	Matrix   Isl.	>	Emb.   Isl.		✓	
	Matrix   Isl.	>	Matrix   Isl.		✓	
	Emb.   Non Isl.	>	Emb.   Isl.		✓	
CNP Island	Matrix   Non Isl.	>	Emb.   Non Isl.		✓	
	Matrix   Non Isl.	=	Matrix   Isl.		✓	
	Matrix   Non Isl.	>	Emb.   Isl.		✓	
	Matrix   Isl.	>	Emb.   Isl.		✓	
	Matrix   Isl.	>	Matrix   Isl.		✓	
	Emb.   Non Isl.	>	Emb.   Isl.		✓	

TL;DR

**Success in all cases but one!**

# Subject Island: Case 1

- (5) a. **What** do you think the speech interrupted ***t***? Obj | Non Island
- b. **What** do you think ***t*** interrupted the show? Subj | Non Island
- c. **What** do you think the speech about global warming interrupted the show about ***t***? Obj | Island
- d. **What** do you think the speech about ***t*** interrupted the show about global warming? Subj | Island

Sprouse et al. (2012)				MG Parser	Clause Type	MaxT	SumS
Subj.   Non Isl.	>	Obj.   Non Isl.		✓	Obj./Non Island	14/ <i>do</i>	19
Subj.   Non Isl.	>	Obj.   Isl.		✓	Subj./Non Island	11/ <i>do</i>	14
Subj.   Non Isl.	>	Subj.   Isl.		✓	Obj./Island	23/ <i>T2</i>	22
Obj.   Non Isl.	>	Obj.   Isl.		✓	Subj./Island	15/ <i>do</i>	20
Obj.   Non Isl.	>	Subj.   Isl.		✓			
Obj.   Isl.	>	Subj.   Isl.		×			

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- (5) a. **What** do you think the speech interrupted ***t***? Obj | Non Island
- b. **What** do you think ***t*** interrupted the show? Subj | Non Island
- c. **What** do you think the speech about global warming interrupted the show about ***t***? Obj | Island
- d. \* **What** do you think the speech about ***t*** interrupted the show about global warming? Subj | Island

Sprouse et al. (2012)				MG Parser	Clause Type	MaxT	SumS
Subj.   Non Isl.	>	Obj.   Non Isl.		✓	Obj./Non Island	14/ <i>do</i>	19
Subj.   Non Isl.	>	Obj.   Isl.		✓	Subj./Non Island	11/ <i>do</i>	14
Subj.   Non Isl.	>	Subj.   Isl.		✓	Obj./Island	23/ <i>T2</i>	22
Obj.   Non Isl.	>	Obj.   Isl.		✓	Subj./Island	15/ <i>do</i>	20
Obj.   Non Isl.	>	Subj.   Isl.		✓			
Obj.   Isl.	>	Subj.   Isl.		✗			

# Subject Island: Case 2

- (6) a. **Who** *t* thinks the speech interrupted the primetime TV show?

Matrix | Non Island

- b. **What** do you think *t* interrupted the primetime TV show?

Emb. | Non Island

- c. **Who** *t* thinks the speech about global warming interrupted the primetime TV show?

Matrix | Island

- d. **What** do you think the speech about *t* interrupted the primetime TV show?

Emb. | Island

Sprouse et al. (2012)			MG Parser		Clause Type	MaxT	SumS
Matrix   Non Isl.	>	Emb.   Non Isl.		✓	Matrix   Non Isl.	5/ <i>C</i>	9
Matrix   Non Isl.	>	Matrix   Isl.		✓	Emb.   Non Isl.	11/ <i>do</i>	14
Matrix   Non Isl.	>	Emb.   Isl.		✓	Matrix   Isl.	11/ <i>T<sub>RC</sub></i>	9
Matrix   Isl.	>	Emb.   Isl.		✓	Emb.   Isl.	17/ <i>T<sub>RC</sub></i>	20
Matrix   Isl.	>	Matrix   Isl.		✓			
Emb.   Non Isl.	>	Emb.   Isl.		✓			



# Processing Asymmetries All the Way Down

A variety of processing insights!

## Across Many Constructions

- ▶ Right > center embedding (Kobele et al. 2012)
- ▶ Crossing > nested dependencies (Kobele et al. 2012)
- ▶ SRC > ORC  
(Graf et al. 2017; De Santo 2020; Fiorini, Chang, De Santo 2023)
- ▶ Priming/Stacked RCs (De Santo 2020, 2022)
- ▶ Postverbal subjects  
(De Santo 2019, 2021; Del Valle & De Santo 2023)
- ▶ Persian attachment ambiguities (De Santo & Shafiei 2019)
- ▶ RC attachment preferences  
(De Santo & Lee 2022; Lee & De Santo 2023)

## Across Languages

- ▶ English, German, Italian, French, Spanish
- ▶ Korean, Japanese, Mandarin Chinese
- ▶ Basque, Persian, ...

# Summary

## Gradience from a categorical MG grammar?

- ▶ The **first** (quantitative) model of this kind!
- ▶ Overall, a success!  $\Rightarrow$  **just** from structural differences!
- ▶ Outlier is expected (and makes predictions!)

## The tip of the iceberg!

- ▶ Modulate range of dependencies
- ▶ Other examples of gradience
- ▶ Cognitive vs. grammatical constraints? (Ferrara-Boston 2012)
- ▶ Syntactic constraints  $\sim$  pruning the parsing space (Stabler 2013, Graf & De Santo 2020)
- ▶ Economy principles (De Santo & Lee 2022)

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# Outline

- 1 Theory Building
- 2 Linguistics and Formal Language Theory
- 3 MG Parsing as a Model of Gradience
- 4 Conclusion**

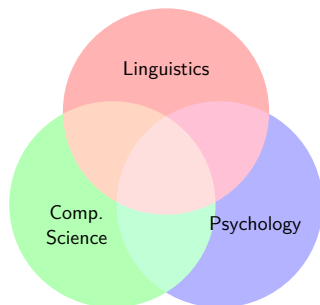
## From the Trees (back) to the Forest

*[...] this is a confusion of two quite separate issues, **simulation and explanation**. [...] What we are **really** interested in [...] is explanation — in developing models that help us **understand how it is that people behave** that way, not merely demonstrating that we can build an artifact that behaves similarly.*

*(Kaplan, 1995)*

- ▶ Invariant properties of phenomena
- ▶ Implementations of verbal theories

# Embracing Multidisciplinary



*Within the program of research proposed here, joint work by linguists, computer scientists, and psychologists could lead to a deeper scientific understanding of the role of language in cognition.*

*(Bresnan 1978: pg. 59)*

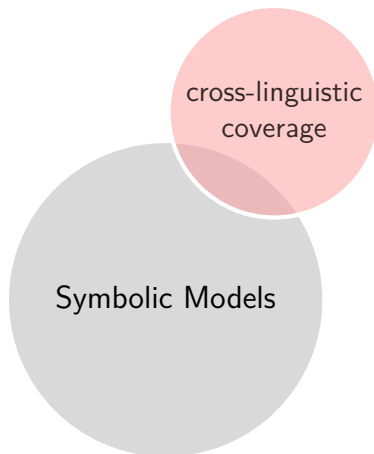
# Looking Ahead: A Collaborative Enterprise



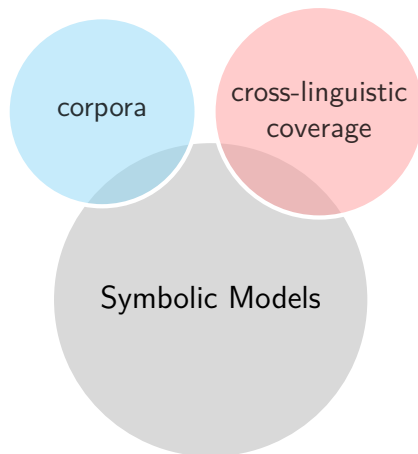
Symbolic Models



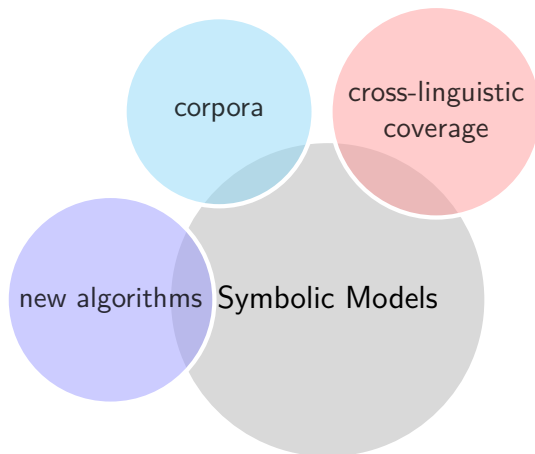
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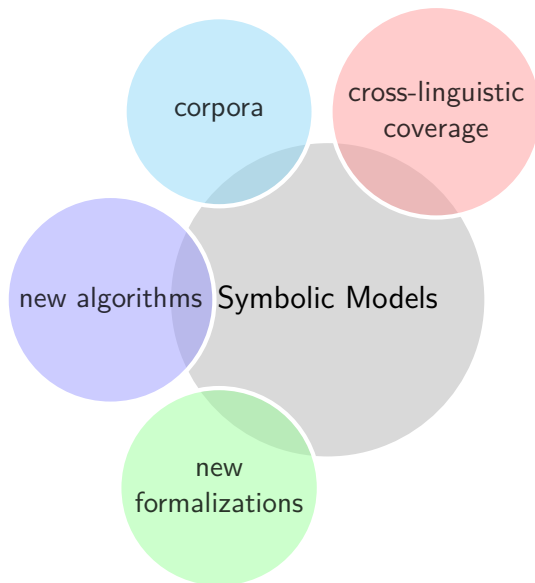
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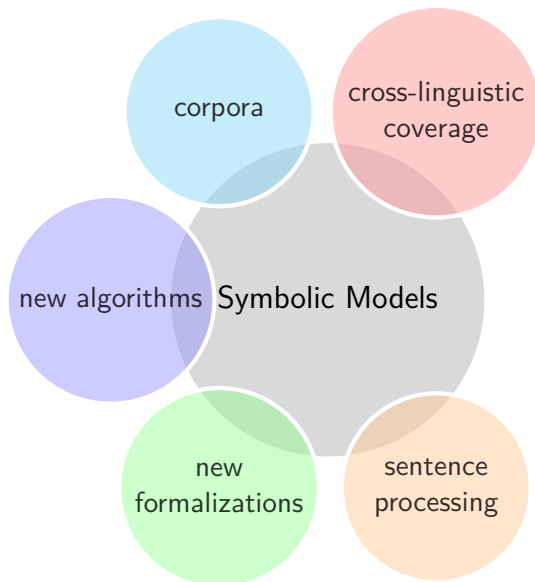
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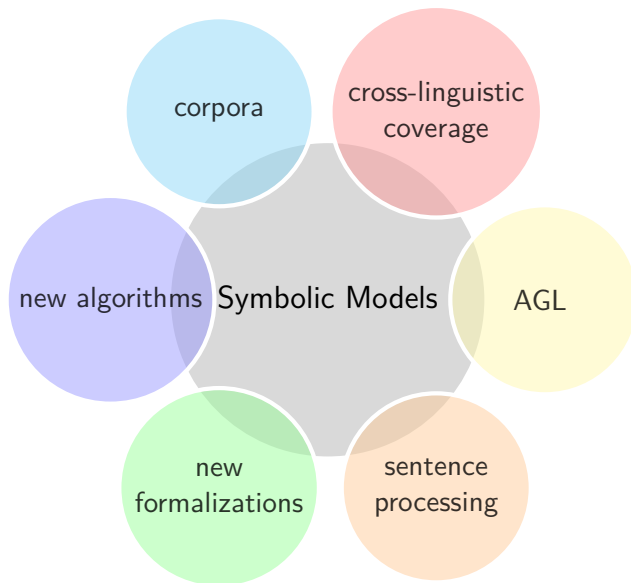
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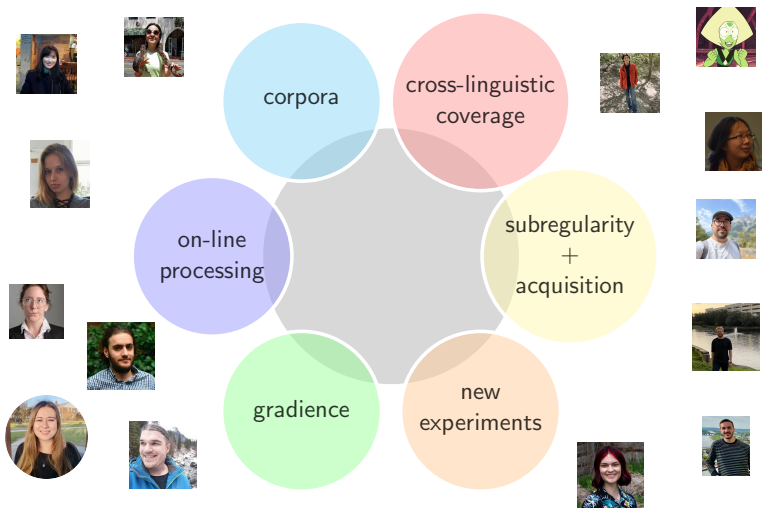
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# Looking Ahead: A Collaborative Enterprise



# Looking Ahead: A Collaborative Enterprise





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- 1 Applegate, R.B. 1972. Ineseno chumash grammar. Doctoral Dissertation, University of California, Berkeley.
- 2 De Santo, A. (2019). Testing a Minimalist grammar parser on Italian relative clause asymmetries. In *Proceedings of CMCL 2019*, June 6 2019, Minneapolis, Minnesota.
- 3 De Santo, A. (2020). MG Parsing as a Model of Gradient Acceptability in Syntactic Islands. In *Proceedings of SCiL 2020*, Jan 2-5, New Orleans.
- 4 De Santo, A. & Aksenova, A. (2021). Learning Interactions of Local and Non-Local Phonotactic Constraints from Positive Input. In *Proceedings of SCiL*
- 5 De Santo, A. and Graf, T. 2019. Structure sensitive tier projection: Applications and formal properties. *Proceedings of FG*.
- 6 De Santo, A. & Rawski, J. (2022). Mathematical Linguistics and Cognitive Complexity. In *Handbook of Cognitive Mathematics* (pp. 1-38).
- 7 Graf, T. and Monette, J. and Zhang, C. (2017). Relative Clauses as a Benchmark for Minimalist Parsing. *Journal of Language Modelling*.
- 8 Kobele, G.M., Gerth S., and Hale. J. (2012). Memory resource allocation in top-down minimalist parsing. In *Formal Grammar*, pages 32–51. Springer.
- 9 Stabler, E.P. (2013). Bayesian, minimalist, incremental syntactic analysis. *Topics in Cognitive Science* 5:611–633.

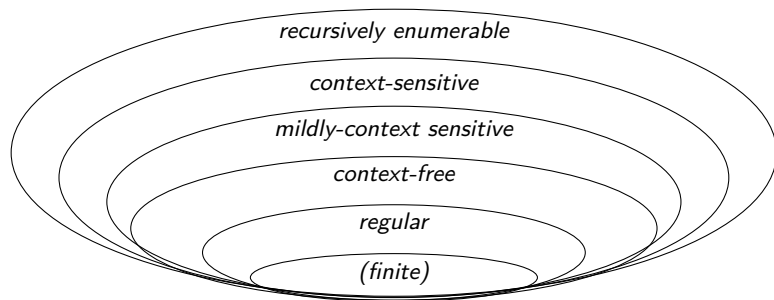
# Appendix

## Kaplan's Full Quote

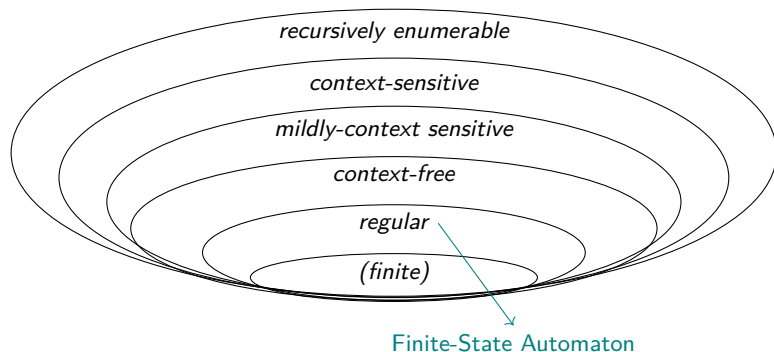
*[...] this is a confusion of two quite separate issues, simulation and explanation. As scientists, we are not merely interested in simulating human behavior [...] What we are really interested in [...] is explanation — in developing models that help us **understand how it is that people behave** that way, not merely demonstrating that we can build an artifact that behaves similarly. [...] We should look for modular theories that account for the observed interactions in terms of the interleaving of information from separate, scientifically comprehensible systems*

*(Kaplan, 1995)*

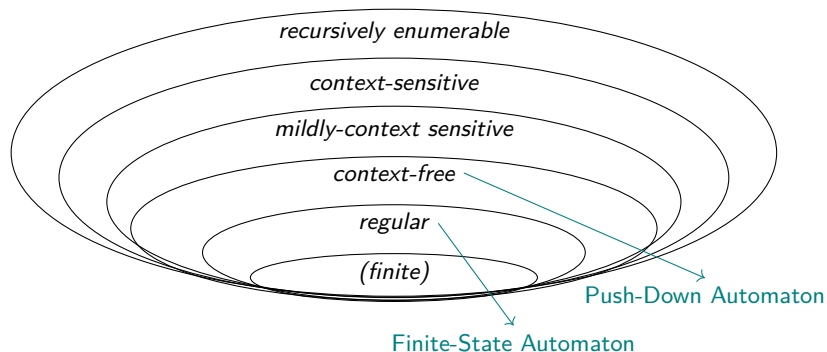
# Chomsky Hierarchy and Automata Theory



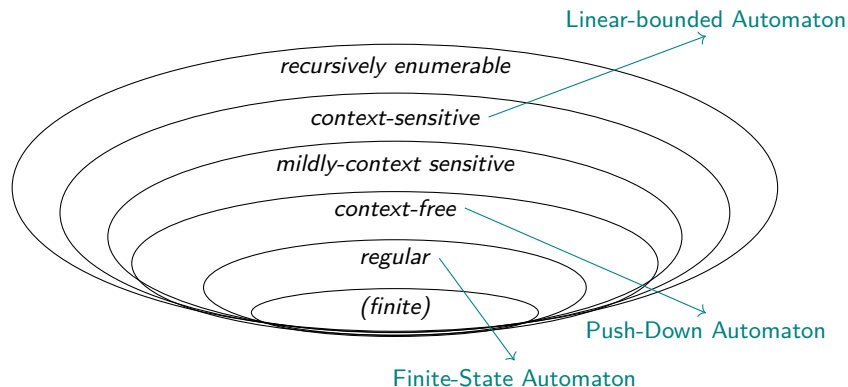
# Chomsky Hierarchy and Automata Theory



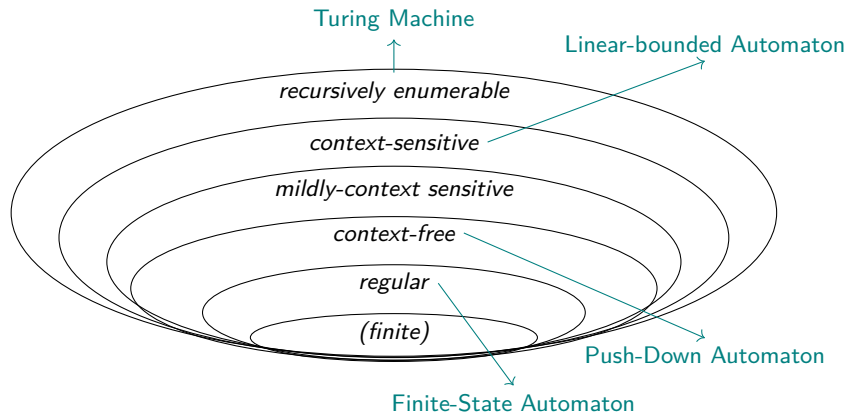
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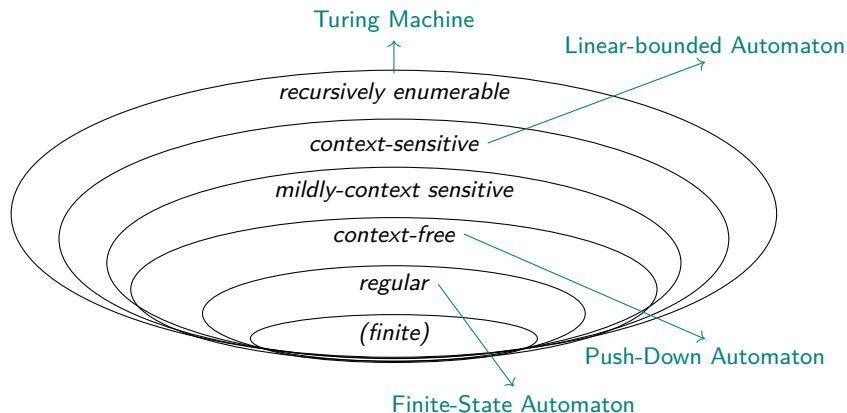


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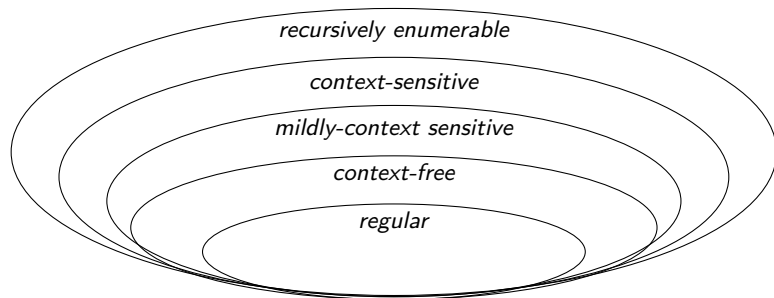
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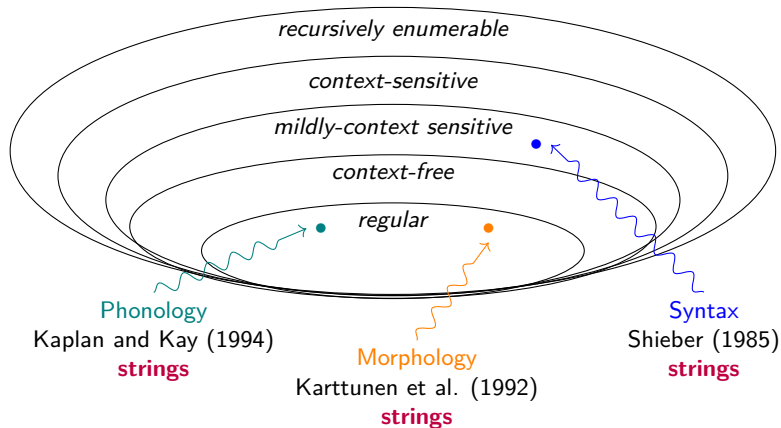
*Automata theoretic classes seem to presuppose [...] specific classes of recognition mechanisms, raising questions about whether these are necessarily relevant to the cognitive mechanisms under study.*

*Rogers & Pullum 2011*

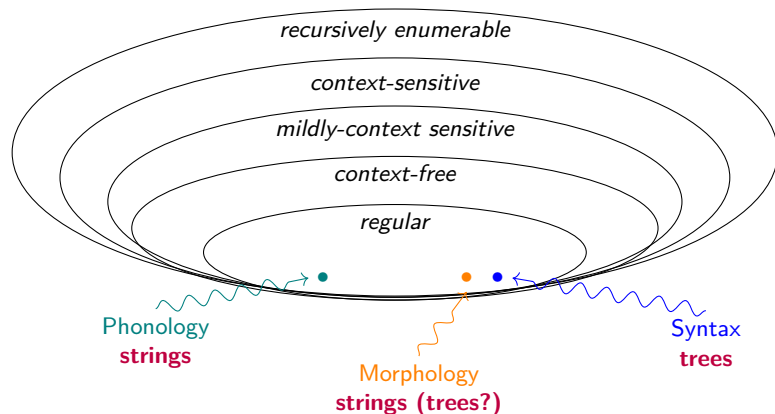
# Cross-domain Parallels



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# Cross-domain Parallels



# Some Insights

## Parallels between phonology and syntax?

- ▶ What would a computational linguist tell you?

Well, it depends!

- ▶ What will I show you?

They are fundamentally similar!

## The Take-Home Message

- ▶ **Two kind of dependencies:** local and non-local
- ▶ The core mechanisms are **the same** cross-domain
- ▶ That is: linguistic dependencies are **local** over the right **structural representations**

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# What about Syntax?

## We need a model for syntax ...

- ▶ Minimalist grammars (MGs) are a formalization of Minimalist syntax. (Stabler 1997, 2011)
- ▶ Operations: **Merge** and **Move**
- ▶ Adopt Chomsky-Borer hypothesis:  
Grammar is just a finite list of feature-annotated lexical items

### Local dependencies in syntax

- ▶ Merge is a **feature-driven** operation:  
category feature  $N^-, D^-, \dots$   
selector feature  $N^+, D^+, \dots$
- ▶ Subcategorization as formalized by Merge is **strictly local**.



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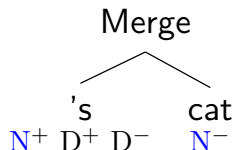
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		's		cat
$N^+$	$D^+$	$D^-$		$N^-$

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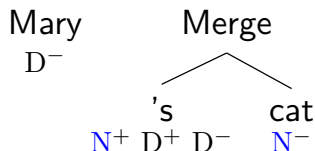
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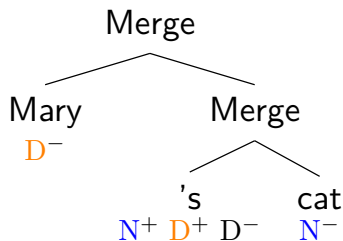
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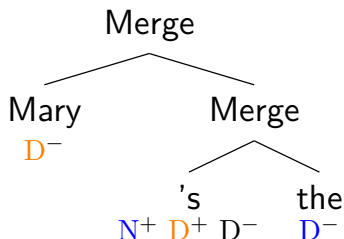
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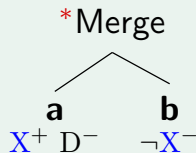


## Merge is SL (Graf 2012)

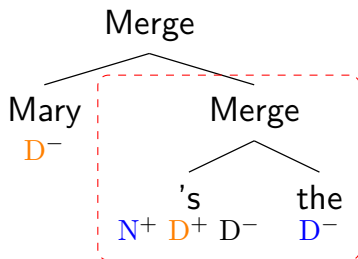


## SL constraints on Merge

- ▶ We lift constraints from **string  $n$ -grams** to **tree  $n$ -grams**
- ▶ We get SL constraints over subtrees.

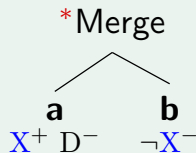


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# Interim Summary

	Local	Data Structure
Phonology	?	?
Syntax	?	?

Local phenomena modeled by  $n$ -grams of bounded size:

- ▶ computationally very simple
- ▶ learnable from positive examples of strings/trees
- ▶ plausible cognitive requirements



# Interim Summary

	Local	Data Structure
Phonology	SL	Strings
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# Interim Summary

	Local	Non-local	Data Structure
Phonology	SL	?	Strings
Syntax	SL	?	Trees

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# TSL Phonology: Accounting for Context

## ► **Unbounded Tone Plateauing in Luganda (UTP)**

No L may occur within an interval spanned by H.

(Hyman 2011)

- (7) a.    **L**HLLLL  
       b.    LLLL**H**L  
       c.    \* **L**HLL**H**L  
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Example

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### Example

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# Accounting for Context [cont.]

## A TSL analysis for UTP (De Santo and Graf 2017):

- ▶ Project every **H**; project **L** iff immediately follows **H**
- ▶ Ban: **HLH**

### Example

*ok* **L H L L L L**

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# Accounting for Context [cont.]

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- ▶ Project every **H**; project **L** iff immediately follows **H**
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### Example

**H**  
 .....  
 ok **L****H** L L L L

\* **L****H** L L **H** L

# Accounting for Context [cont.]

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HL
   
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 .....  
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**H** **L**  
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### Example

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 .....  
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### Example

.....  
 ok **L** **H** **L** **L** **L** **L**

**H** **L**   **H** **L**  
 .....  
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# TSL for Phonology

## Most non-local dependencies in phonology are TSL

- ▶ Linguistically natural (Goldsmith 1976)
- ▶ Captures wide range of phonotactic dependencies (McMullin 2016)
- ▶ Provably correct and efficient learning algorithms (Jardine and McMullin 2017)
- ▶ Rules out unattested patterns (cf. Lai 2015, Aksenova et al. 2016, Graf & De Santo 2019, a.o.)

What about syntax?

# TSL for Phonology

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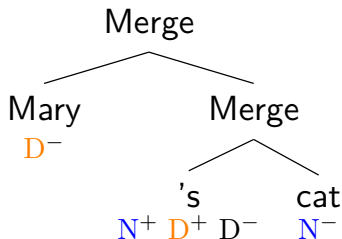
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**What about syntax?**

# Non-Local Dependencies in Syntax

Let's stick to core operations:

- ▶ Move
- ▶ Merge?

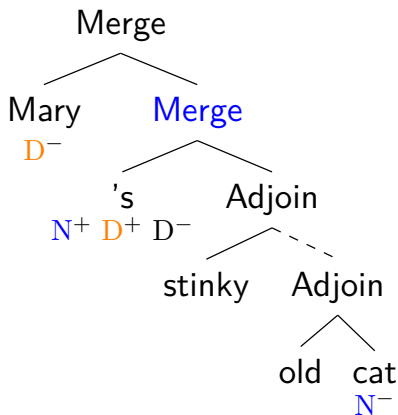




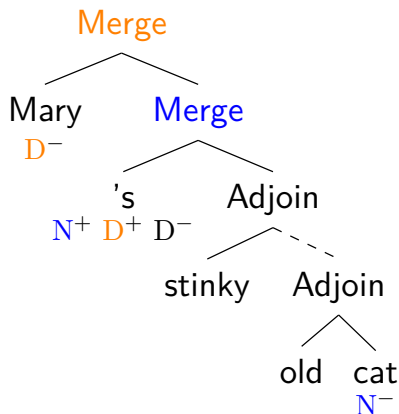
# Non-Local Dependencies in Syntax

Let's stick to core operations:

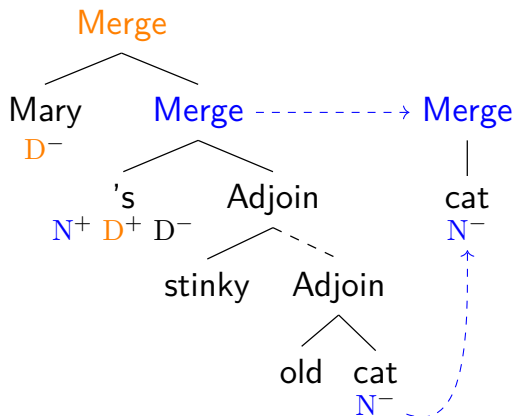
- ▶ Move
- ▶ **Merge**: Unbounded adjunction  
Frey and Gärtner (2002); Graf (2017)



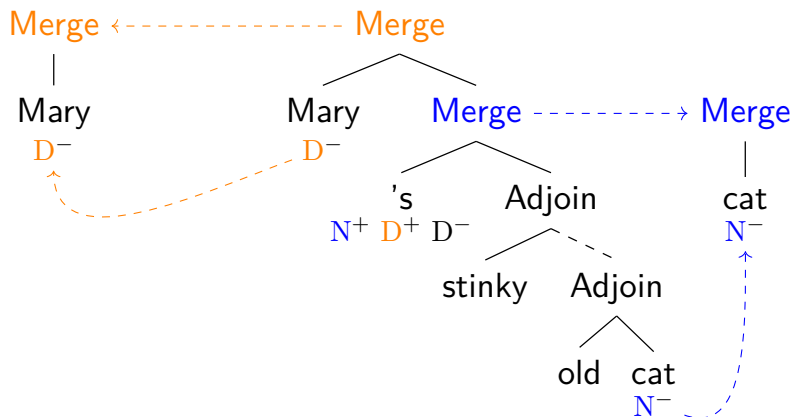
# TSL over Trees: Projecting Tiers



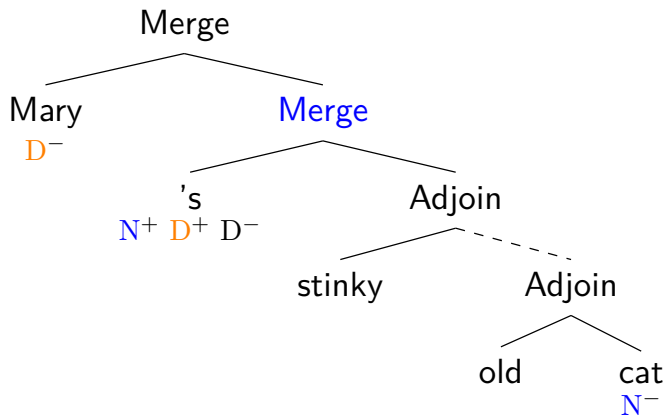
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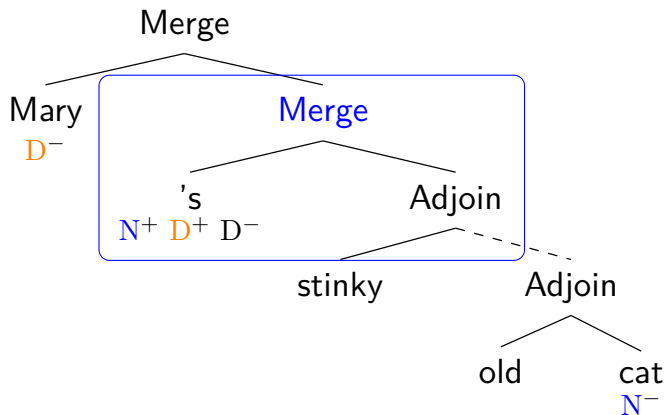


# Merge with Adjunction is TSL



A TSL grammar for Merge

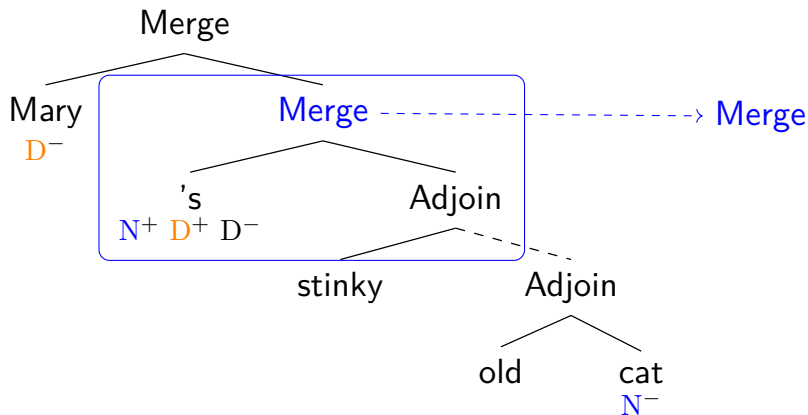
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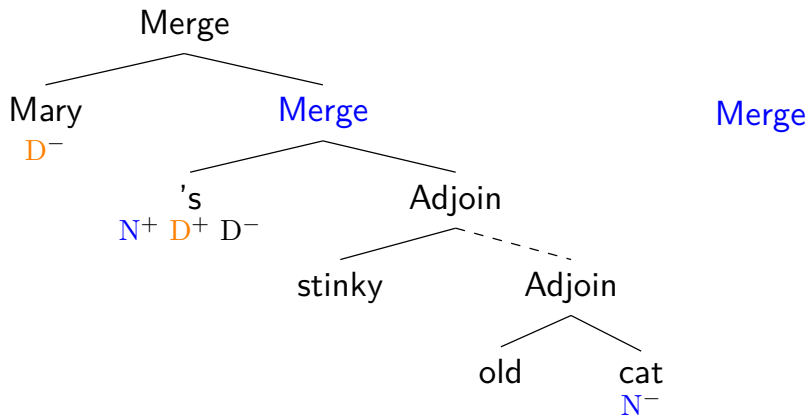
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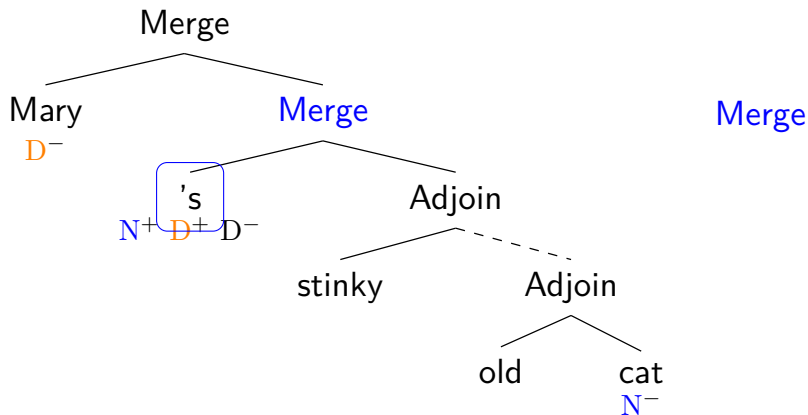


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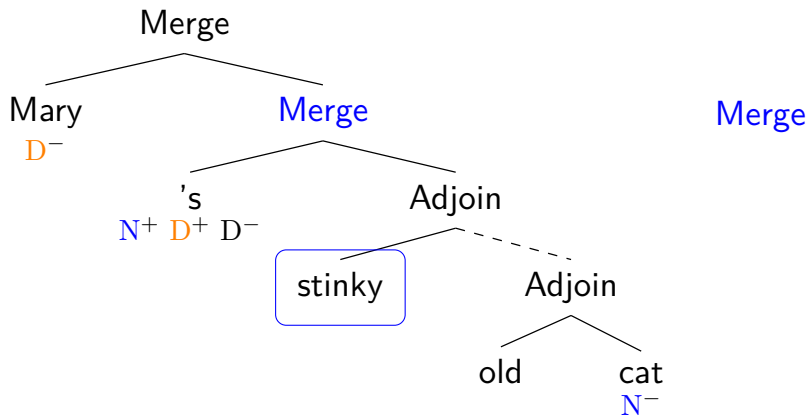
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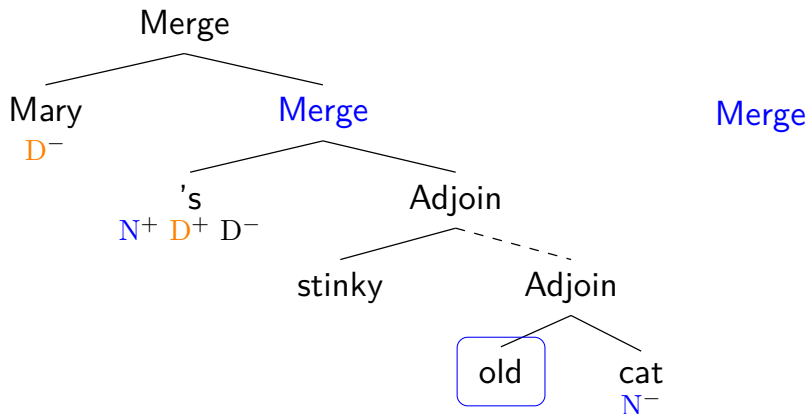
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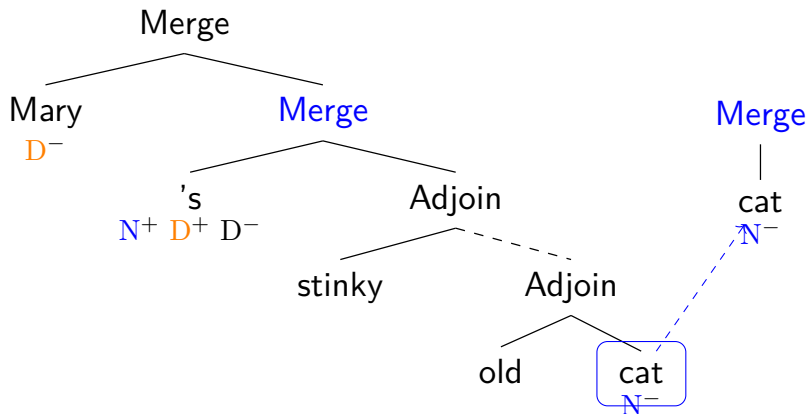
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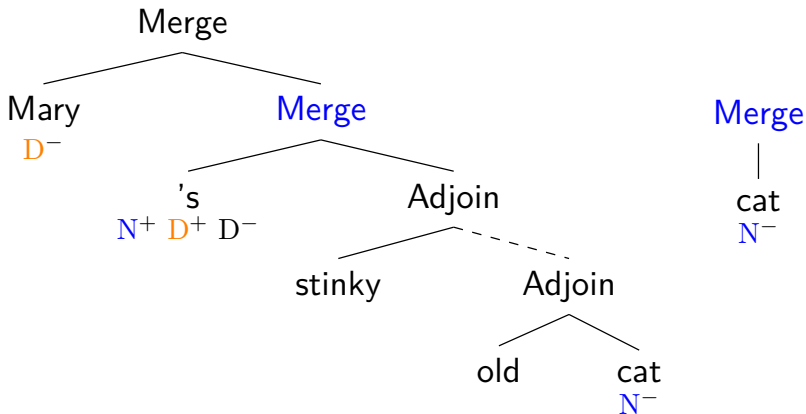
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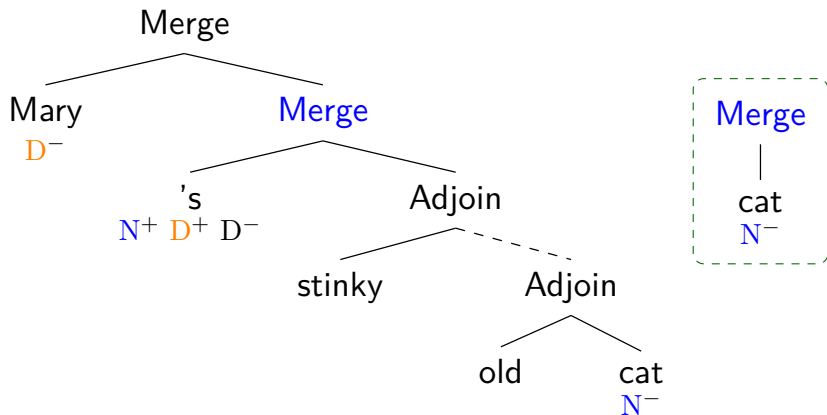
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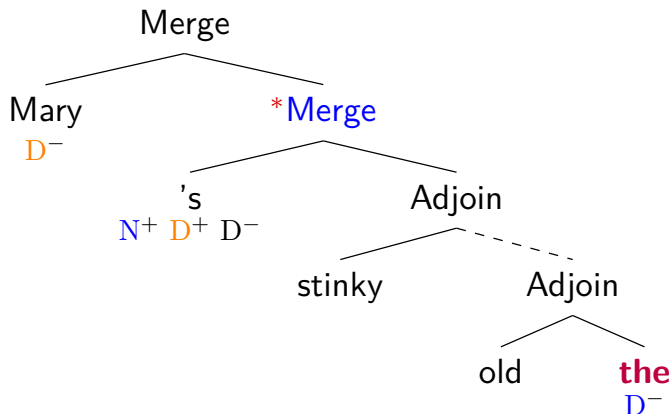
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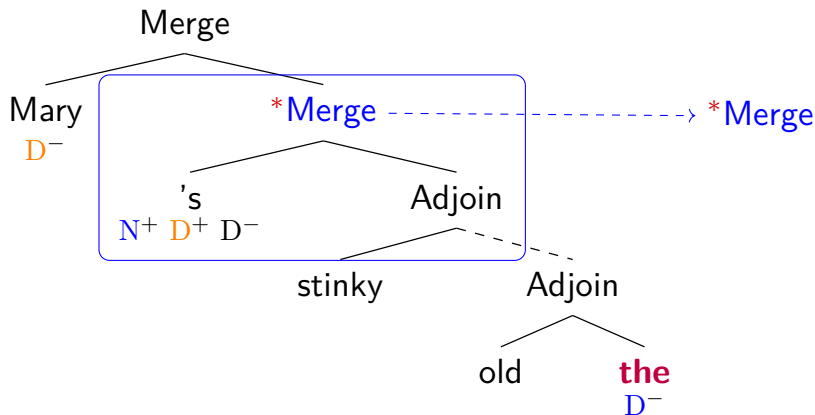
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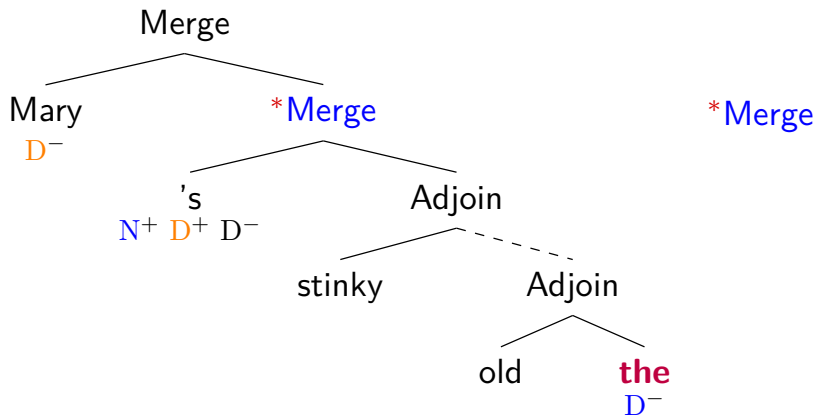


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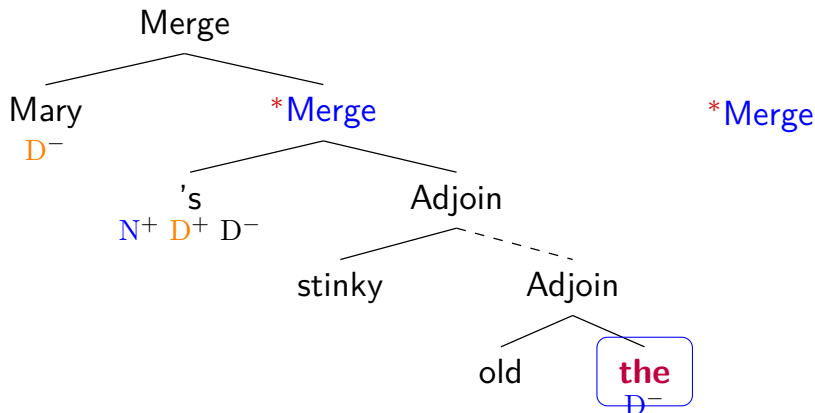
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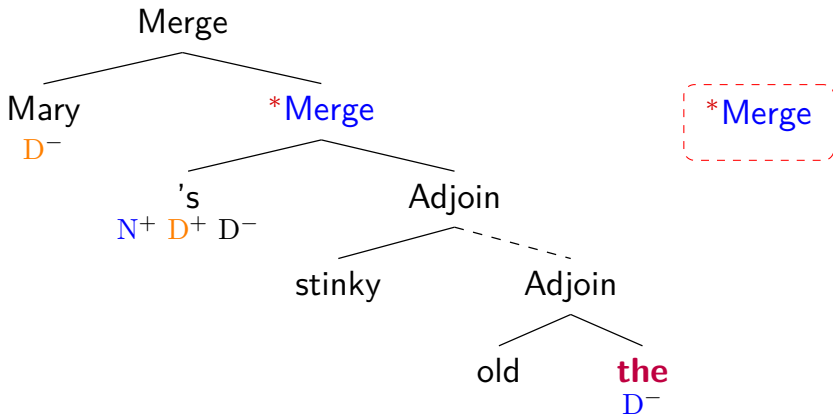
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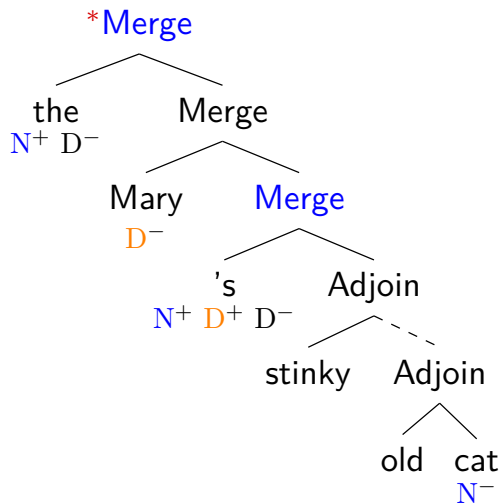
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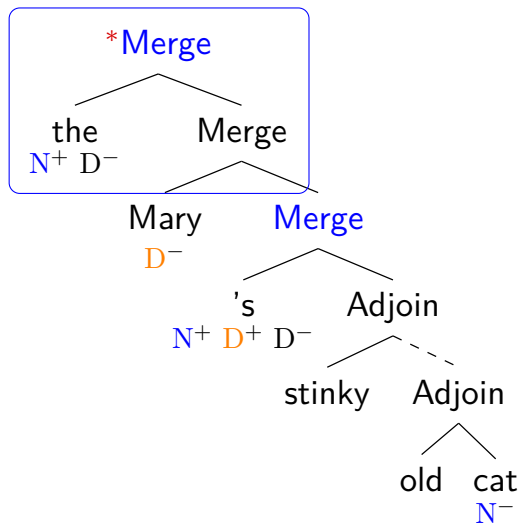
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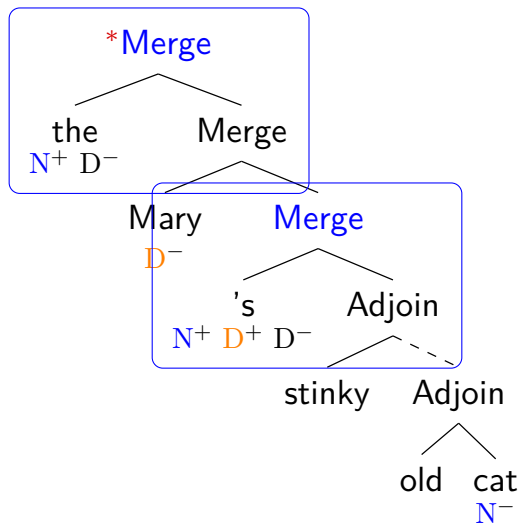
# TSL Merge: Understanding the Constraint



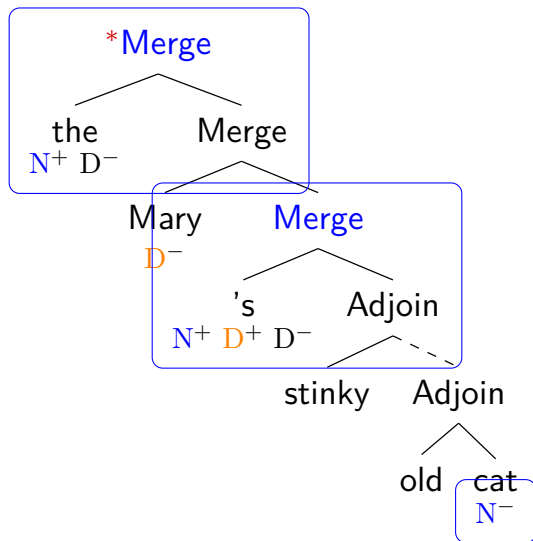
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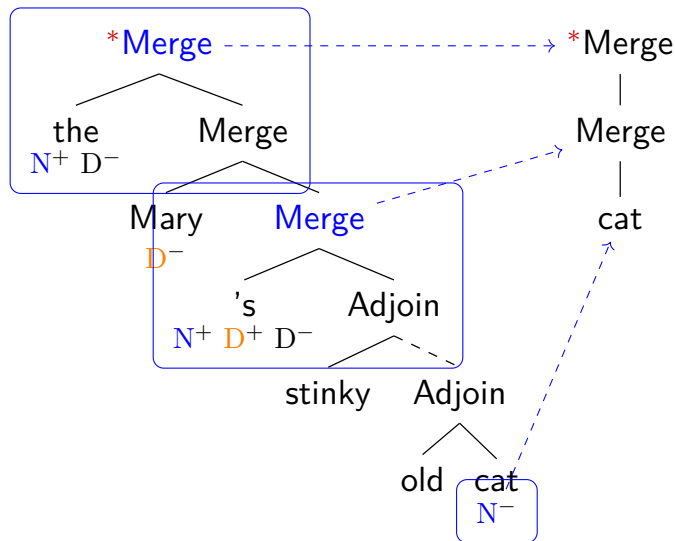
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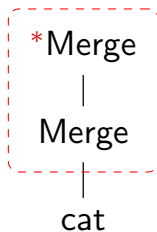
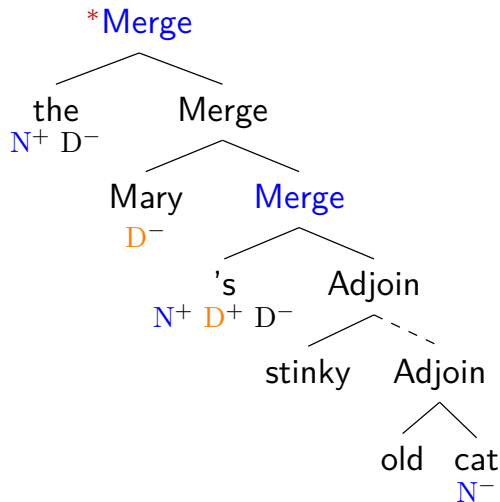


# TSL Merge: Understanding the Constraint





# TSL Merge: Understanding the Constraint



# Parallels Between Phonology And Syntax

	Local	Non-local
<b>Phonology</b>	?	?
<b>Syntax</b>	?	?

► **Relativized Locality:**

Non-local dependencies are local over a simple relativization domain.

## Strong Cognitive Parallelism Hypothesis

Phonology, (morphology), and syntax have the **same subregular complexity** over their respective **structural representations**.

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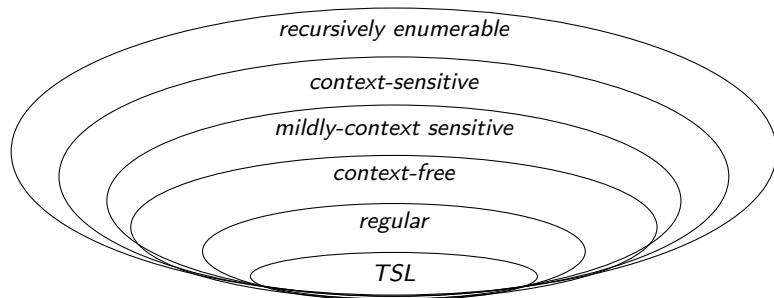
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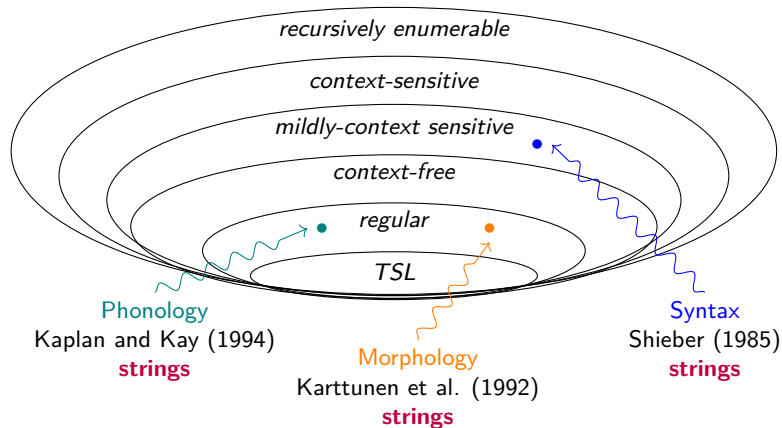
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# A Bird's-Eye View of the Framework

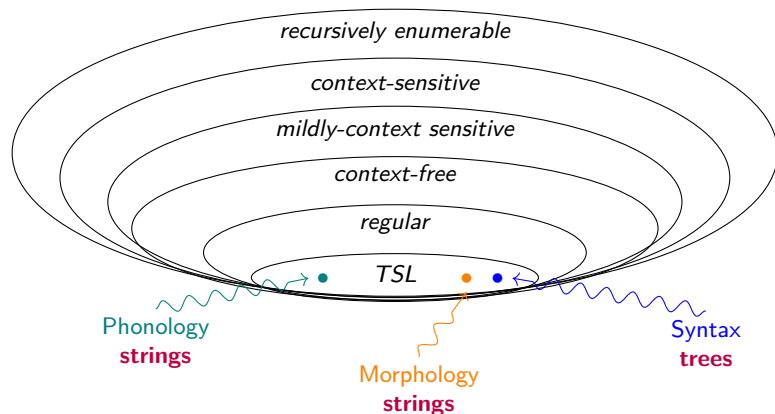


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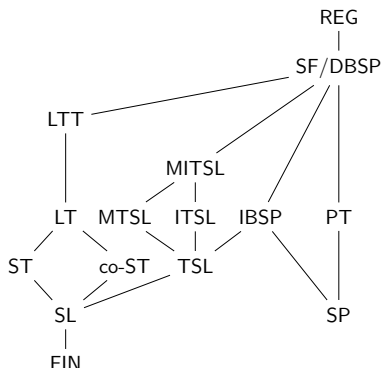




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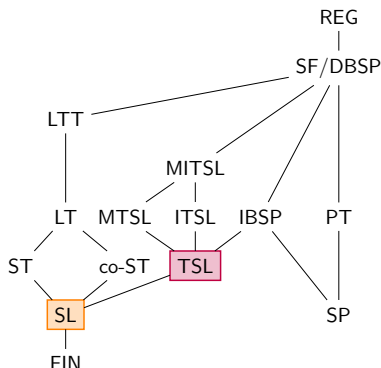


# Refining the Hierarchy via Typological Insights



- ▶ The goal is not identifying a single “correct” class
- ▶ Pinpoint fundamental properties of the patterns:  
SL:  $\triangleleft$  , TSL:  $\triangleleft_T$ , etc

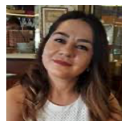
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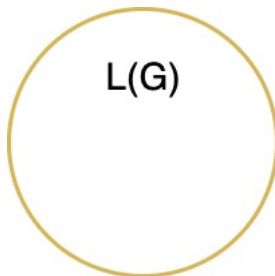
# Syntax beyond Merge and Move

- ▶ regular tree languages  
(Michaelis 2004; Kobele et al. 2007)
- ▶ subregular **operations** (Graf 2018)
- ▶ subregular **dependencies/constraints**  
(Vu et al. 2019; Shafiei and Graf 2019)
- ▶ tree automata and **parsing restrictions**  
(Graf & De Santo 2020)



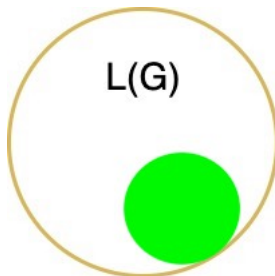
# Artificial Grammar Learning (AGL)

- ▶ Can be used to test implicit learning abilities (Reber, 1976)



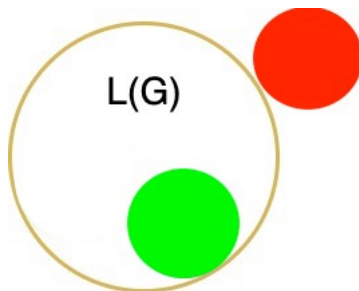
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# Reber (1976)

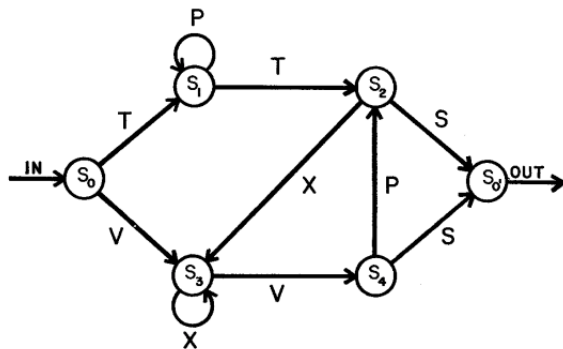


FIG. 1. Schematic state diagram of the grammar used to generate the grammatical stimulus items.

- ▶ Stimuli generated from an FST or randomly
  - ▶ 28 sentences per group, in sets of four sentences each
  - ▶ Participants asked to reproduce the sentences in a group
  - ▶ Participants informed of correct/incorrect reproductions, but not of error type



## Reber (1976) [cont.]

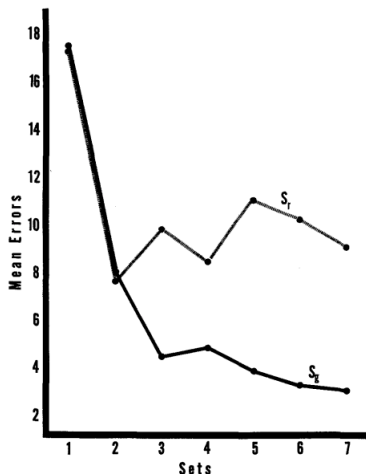
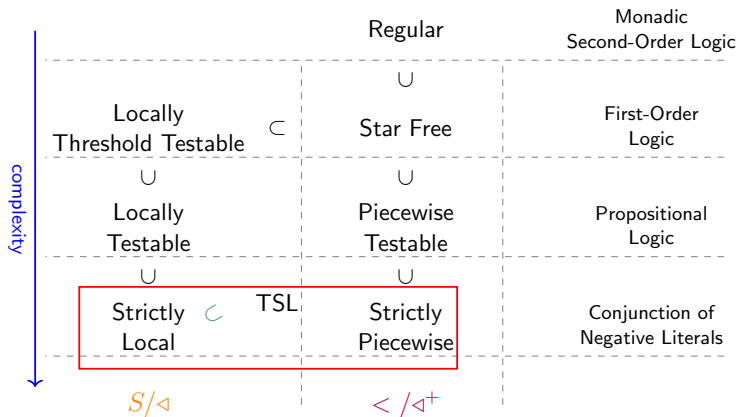


Fig. 2. Mean number of errors to criterion on each of the seven learning sets.

- ▶ Stimuli generated from an FST or randomly
  - ▶ Significant differences between learning trajectories across participant group

# Testing Subregular Predictions




# Example: Attested vs. Unattested Patterns

## Attested: Unbounded Sibilant Harmony


- ▶ Every sibilant needs to harmonize

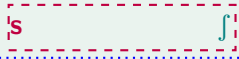
  
 \* \$ha **s**xintilawʃ\$

  
 ok \$haʃxintilawʃ\$

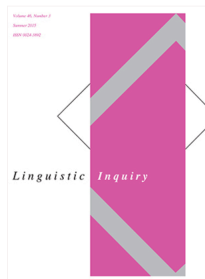
## Unattested: First-Last Harmony

- ▶ Harmony only holds between initial and final segments

  
 ok \$ha **s**xintilawʃ\$

  
 \* \$ **s**atxintilawʃ\$

# Lai (2015)



## Learnable vs. Unlearnable Harmony Patterns

Regine Lai

Posted Online July 09, 2015

[https://doi.org/10.1162/LING\\_a\\_00188](https://doi.org/10.1162/LING_a_00188)

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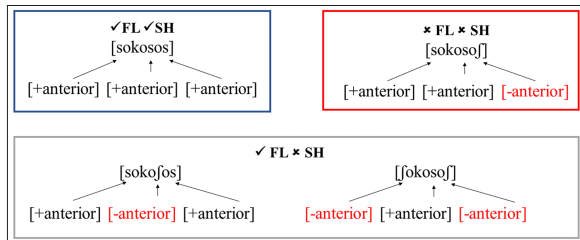
**Linguistic Inquiry**

Volume 46 | Issue 3 | Summer 2015

p.425-451

**Keywords:** phonotactics, learnability, computational phonology, formal theory, typology, dependencies

## Lai (2015): Stimuli



**Figure 3:** Comparison of SH and FL stimuli.

## Lai (2015): Stimuli

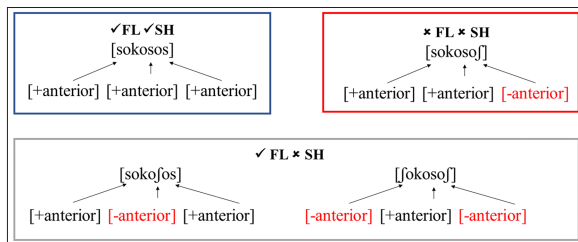


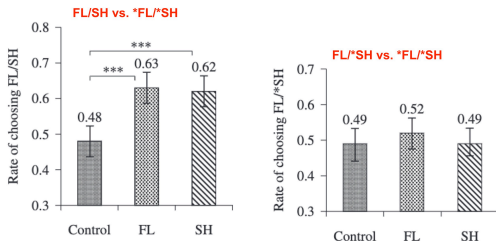
Figure 3: Comparison of SH and FL stimuli.

Table 6

Predicted results with respect to the control group for each test pairing if Sibilant Harmony and First-Last Assimilation grammars were internalized

Conditions	Pairs		
	FL/*SH vs. *FL/*SH (e.g., [s ... ʃ ... s] vs. [s ... s ... ʃ]) Rate of FL/*SH	FL/SH vs. *FL/*SH (e.g., [s ... s ... s] vs. [s ... s ... ʃ]) Rate of FL/SH	FL/SH vs. FL/*SH (e.g., [s ... s ... s] vs. [s ... ʃ ... s]) Rate of FL/SH
SH	~ Control	> Control	> Control
FL	> Control	> Control	~ Control

# Lai (2015): Results



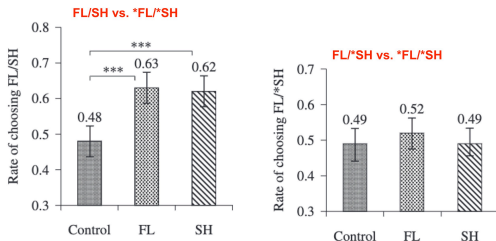
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► See Avcu and Hestvik (2020), Avcu et al. (2019) for replications

# Lai (2015): Results



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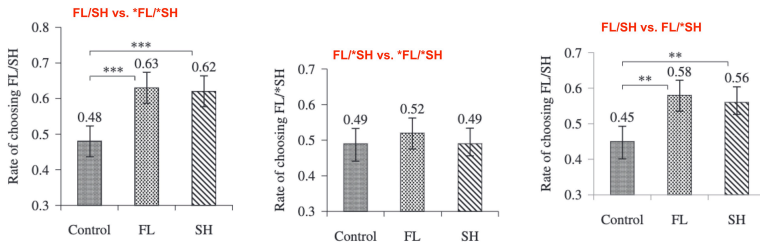
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# Lai (2015): Full Results



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	Rate of FL/*SH	Rate of FL/SH	Rate of FL/SH
SH	~ Control	> Control	> Control
FL	> Control	> Control	~ Control

# AGL and Syntax/Semantics

*distinctions between mechanisms for recognizing non-Finite-State stringsets depend on the way in which the additional structure, beyond the string itself, is organized; these are issues that show up in the analysis of the string, not in its form as a sequence of events.*

*Rogers & Pullum 2011*

In other words:

- ▶ Questions of complexity confounded by representations
- ▶ Questions of representations confounded by procedures

# AGL and Syntax/Semantics

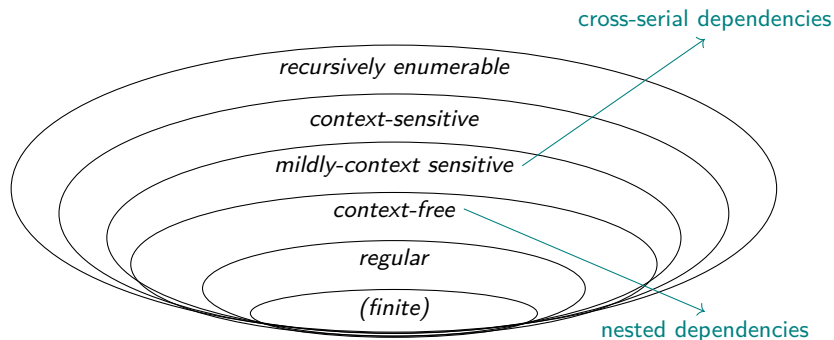
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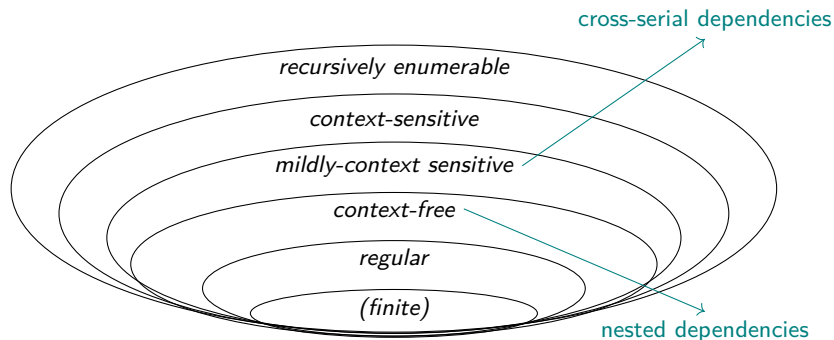
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# Syntactic Expressivity



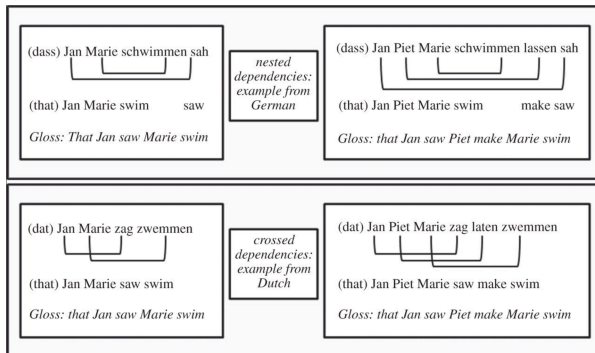
- ▶ cross-serial preferred over nested (Bach et al. 1986)
- ▶ against predictions from the CH?  
(Chesi & Moro 2014; de Vries et al. 2012)

# Syntactic Expressivity



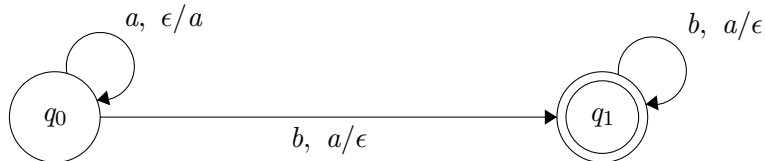
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# Expressivity vs. Procedures



- ▶ cross-serial preferred over nested (Bach et al. 1986)
- ▶ against predictions from the CH?  
(Chesi & Moro 2014; de Vries et al. 2012)
- ▶ BUT: this can easily be derived via processing mechanisms  
(Savitch 1989; Joshi, 1990; Rainbow and Joshi, 1994)
- ▶ recognition complexity requires a precise theory of parsing cost

# AGL and Syntax/Semantics [cont.]

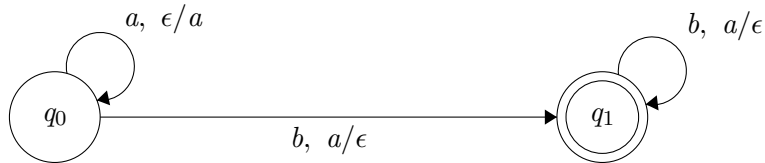


- ▶  $A^n B^n$  does not necessarily imply a proper stack  
a PDA with a single counter is enough (Counter Machines)
- ▶ Same for the language of strings of **well-nested parentheses**
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Complicated questions:

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# AGL and Syntax/Semantics [cont.]



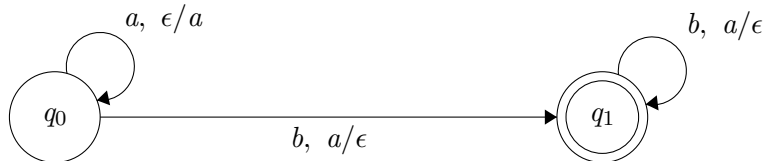
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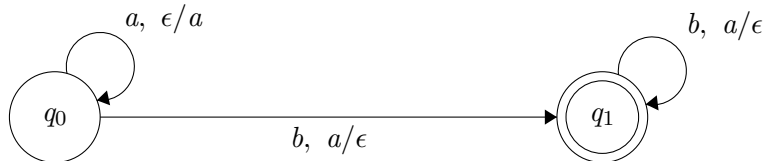


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# A Plethora of Testable Predictions

## Observation

- ▶ Attested patterns **A** and **B** are TSL.
- ▶ But combined pattern **A+B** is not TSL.

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## Morphotactics as Tier-Based Strictly Local Dependencies

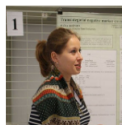
Alëna Aksënova   Thomas Graf   Sedigheh Moradi

## Example: Compounding Markers

- ▶ Russian has an infix **-o-** that may occur between parts of compounds.
- ▶ Turkish has a single suffix **-sı** that occurs at end of compounds.

(8) vod    **-o-**    voz    **-o-**    voz  
 water -COMP- carry -COMP- carry  
 'carrier of water-carriers'

(9) türk    bahçe    kapı    **-sı**    (\***-sı**)  
 turkish garden gate -COMP (\*-COMP)  
 'Turkish garden gate'



## Example: Compounding Markers [cont.]

- ▶ Russian and Turkish are TSL.

	<b>Tier<sub>1</sub></b>	COMP affix and stem edges #
<b>Russian</b>	<i>n</i> -grams	oo, \$o, o\$
<b>Turkish</b>	<i>n</i> -grams	sisi, \$si, si#

- ▶ The combined pattern would yield **Ruskish**: stem<sup>*n*+1</sup>-si<sup>*n*</sup>
- ▶ This pattern is not regular and hence **not TSL either**.
- ▶ **Hypothesis** (Aksenova et al, 2016)  
If a language allows unboundedly many compound affixes, they are **infixes**.

### Testable Predictions

- ▶ Can naive subjects learn Russian-like, Turkis-like, and Ruskish-like compounding?

# Complexity as a Magnifying Lens

- ▶ We can compare patterns and predictions across classes
- ▶ We can also compare patterns within a same class

## Proceedings of the Society for Computation in Linguistics

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## Formal Restrictions On Multiple Tiers

Alena Aksenova

*Stony Brook University*, [alena.aksenova@stonybrook.edu](mailto:alena.aksenova@stonybrook.edu)

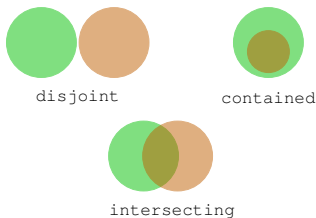
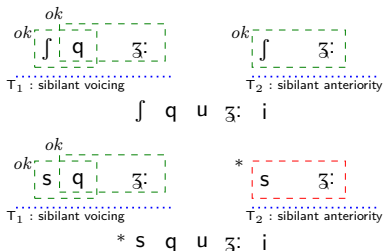
Sanket Deshmukh

*Stony Brook University*, [sanket.deshmukh@stonybrook.edu](mailto:sanket.deshmukh@stonybrook.edu)



# Testing Harmony Systems

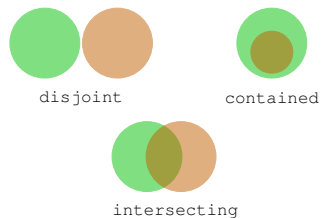
- ▶ We can also account for multiple processes
- ▶ Thus we can cover the complete phonotactics of a language



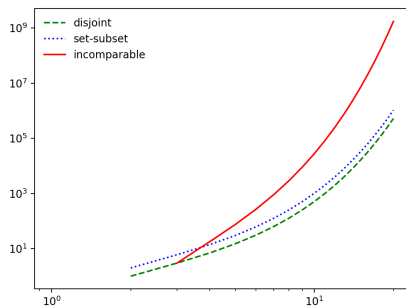
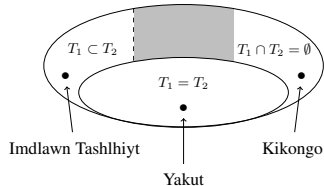
**Figure 2:** Theoretically possible tier alphabet relations



# Testing Harmony Systems (cont.)



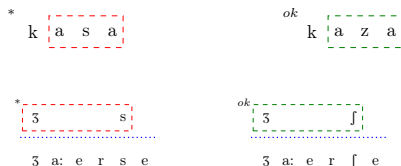
**Figure 2:** Theoretically possible tier alphabet relations



**Figure 7:** Growth of number of partitions of sets containing up to 20 elements (loglog scale)

# The Fallacy of Generalization

- Imagine we want to test the ability to learn long-distance dependencies:



- Assuming an alphabet  $\Sigma = \{a, b, c, d, e\}$ , the training samples could look like the following:

$$L_{loc} = \{abcd, aabcd, baacd, bcaae, \dots\}$$

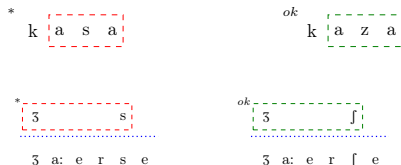
$$L_{dist} = \{abacd, bacad, bcada, bcaea, \dots\}$$

What happens if we test on stimuli with similar distances?

$$L_{test} = \{abcad, abcad, bacda, abcea, \dots\}$$

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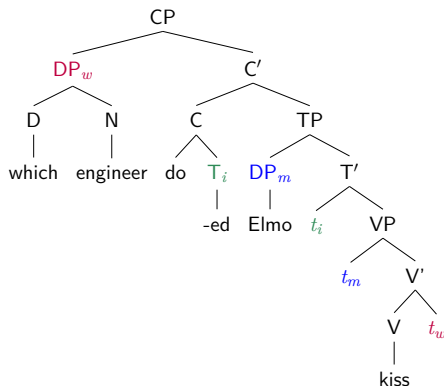
# Why MGs?

- 1 Vast analytical coverage
  - ▶ MGs handle virtually all analyses in the generative literature
- 2 Centrality of derivation trees
  - ▶ MGs can be viewed as CFGs with a more complicated mapping from trees to strings
- 3 Simple parsing algorithms
  - ▶ Variant of a recursive descent parser for CFGs  
⇒ cf. TAG (Rambow & Joshi, 1995; Demberg, 2008)

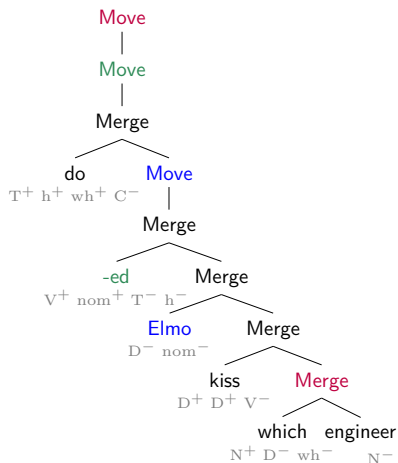
## Some Important Properties of MGs

- ▶ MGs are weakly equivalent to MCFGs and thus mildly context-sensitive. (Harkema 2001, Michaelis 2001)
- ▶ But we can decompose them into two finite-state components: (Michaelis et al. 2001, Kobele et al. 2007, Monnich 2006)
  - ▶ a regular language of well-formed derivation trees
  - ▶ an MSO-definable mapping from derivations to phrase structure trees
- ▶ **Remember:** Every regular tree language can be re-encoded as a CFG (with more fine-grained non-terminal labels). (Thatcher 1967)

# Fully Specified Derivation Trees



Phrase Structure Tree



Derivation Tree

# Technical Fertility of MGs

MGs can accommodate the full syntactic toolbox:

- ▶ sideways movement (Stabler, 2006; Graf 2013)
- ▶ affix hopping (Graf 2012; Graf2013)
- ▶ clustering movement (Gartner & Michaelis 2010)
- ▶ tucking in (Graf 2013)
- ▶ ATB movement (Kobebe 2008)
- ▶ copy movement (Kobebe 2006)
- ▶ extraposition (Hunter & Frank 2014)
- ▶ Late Merge (Kobebe 2010; Graf 2014)
- ▶ Agree (Kobebe 2011; Graf 2011)
- ▶ adjunction (Fowlie 2013; Hunter 2015)
- ▶ TAG-style adjunction (Graf 2012)

# Why These Metrics?

- ▶ These complexity metrics are all related to **storage cost** (cf. Gibson, 1998)
- ▶ We could implement alternative ones (cf. Ferrara-Boston, 2012)
  - ▶ number of bounding nodes / phases
  - ▶ surprisal
  - ▶ feature intervention
  - ▶ status of discourse referents
  - ▶ integration, retrieval, ...
- ▶ We want to keep the model **simple** (but not **trivial**):
  - ▶ Tenure and Size only refer to the geometry of the derivation
  - ▶ they are sensitive the specifics of tree-traversal (cf. node-count; Hale, 2001)



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## Technical details!

- ▶ String-driven recursive descent parser (Stabler 2013)

▶ ● Who ● does ● Salem ● T ●  
mock

- step 1 CP is conjectured
- step 2 CP expands to C'
- step 3 C' expands to does and TP
- step 4 TP expands to Salem and T'
- step 5 T' expands to T and VP
- step 6 VP expands to mock and who
- step 7 who is found
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$$\begin{array}{c} {}^1CP_2 \\ | \\ {}^2C' \end{array}$$

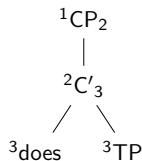
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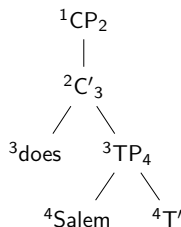
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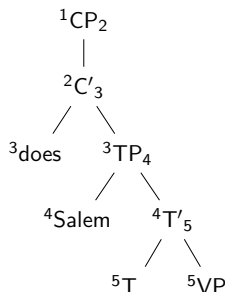
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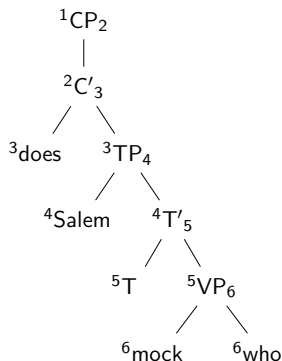
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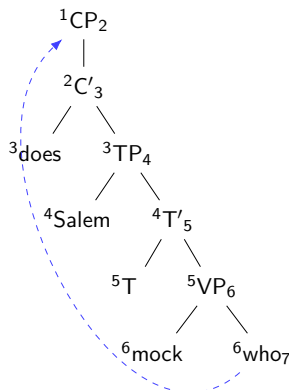
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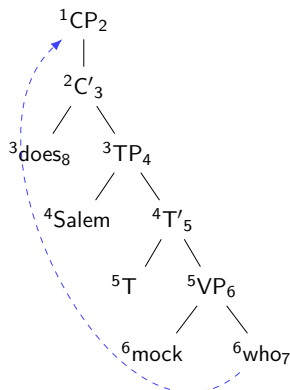
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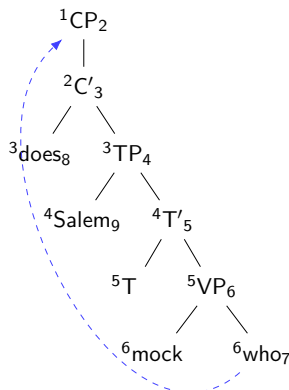
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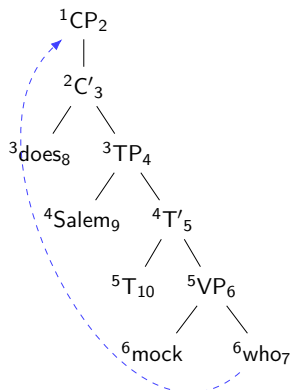
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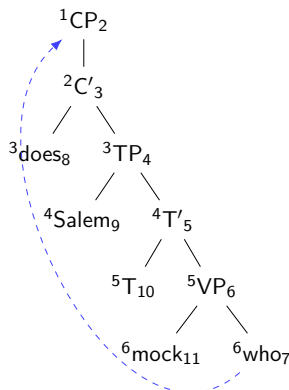
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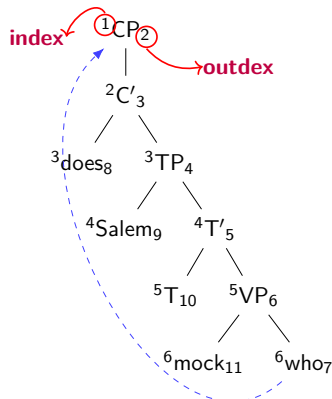
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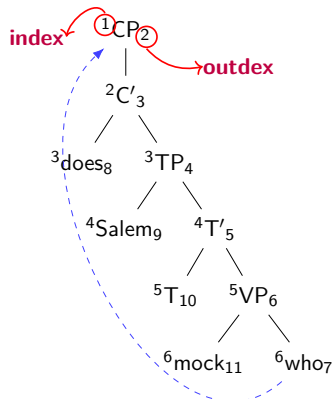
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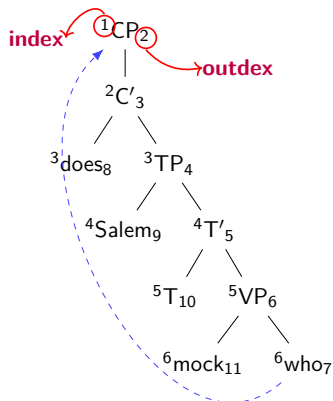
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**Index and Outdex are our connection to memory!**

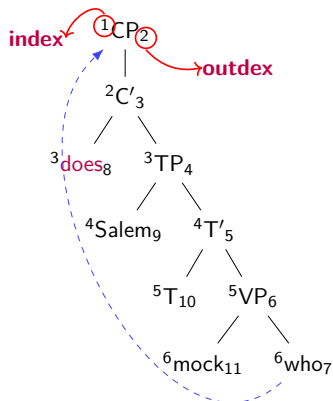
# Computing Metrics: An Example



**Tenure** how long a node is kept in memory



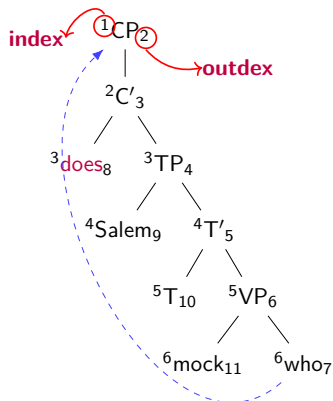
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$$\text{Tenure}(\text{does}) = 8 - 3 = 5$$

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**Tenure** how long a node is kept in memory

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$$\text{MaxTenure} = \max\{\text{Tenure}(\text{does}), \text{Tenure}(\text{Salem}), \dots\} = 5$$

# A Case Study: Italian Postverbal Subjects

## Asymmetries in Italian Relative Clauses

Italian conforms to the general cross-linguistic preference for SRC over ORC (Adani et al. 2010; Arosio et al. 2018)

- (10) Il cavallo che ha inseguito i leoni  
 The horse that has chased the lions  
 “The horse that chased the lions” **SRC**
- (11) Il cavallo che i leoni hanno inseguito  
 The horse that the lions have chased  
 “The horse that the lions chased” **ORC**

**SRC > ORC**

## Postverbal Subjects and Ambiguity

Italian allows for postverbal subjects, making some sentences ambiguous (De Vincenzi 1991):

(12) Il cavallo che ha inseguito il leone

The horse that has chased the lion

a. “The horse that chased the lion”

**SRC**

b. “The horse that the lion chased”

**ORC<sub>p</sub>**

**SRC > ORC<sub>p</sub>**

Agreement can disambiguate:

(13) Il cavallo che hanno inseguito i leoni

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The horse that have chased the lions

“The horse that the lions chased”

**ORC<sub>p</sub>**

## Postverbal Subjects and Ambiguity

Italian allows for postverbal subjects, making some sentences ambiguous (De Vincenzi 1991):

(12) Il cavallo che ha inseguito **il leone**

The horse that has chased the lion

a. “The horse that chased the lion”

**SRC**

b. “The horse that **the lion** chased”

**ORC<sub>p</sub>**

**SRC > ORC<sub>p</sub>**

Agreement can disambiguate:

(13) Il cavallo che hanno inseguito i leoni

The horse that have chased the lions

“The horse that the lions chased”

**ORC<sub>p</sub>**

# Asymmetries in Italian Relative Clauses

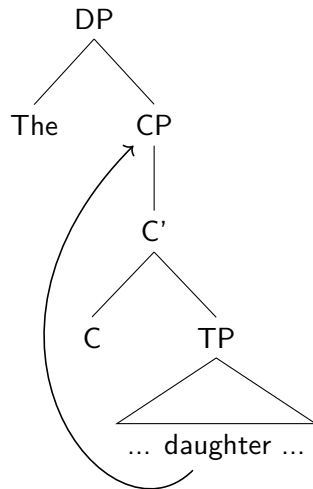
- |     |   |             |
|-----|---|-------------|
| (1) | Il cavallo che ha inseguito i leoni<br>The horse that has chased the lions<br>“The horse that chased the lions”     | <b>SRC</b>  |
| (2) | Il cavallo che i leoni hanno inseguito<br>The horse that the lions have chased<br>“The horse that the lions chased” | <b>ORC</b>  |
| (4) | Il cavallo che hanno inseguito i leoni<br>The horse that have chased the lions<br>“The horse that the lions chased” | <b>ORCp</b> |

Processing Asymmetry (De Vincenzi 1991, Arosio et al. 2018, a.o.)

**SRC > ORC > ORCp**

# Kayne's Promotion Analysis (Kayne 1994)

- ▶ RC is selected by an external  $D^0$
- ▶ the RC head is a nominal constituent
- ▶ the RC head raises from its base position to [Spec, CP]

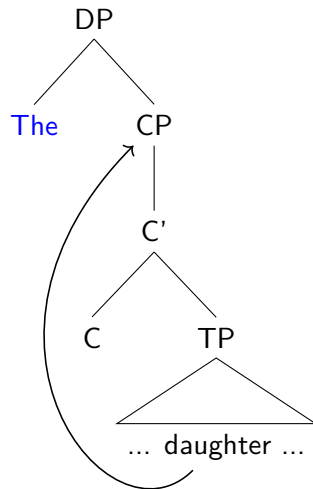


$[_{DP} \text{The } [_{CP} \text{daughter}_i [ \text{that } t_i \text{ was on the balcony } ]]]$



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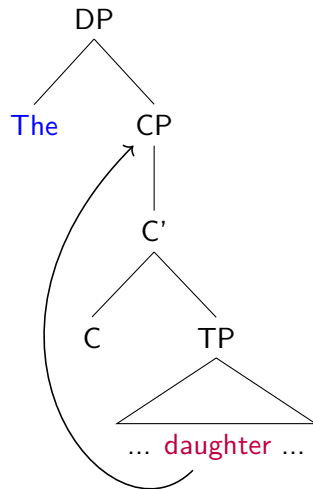
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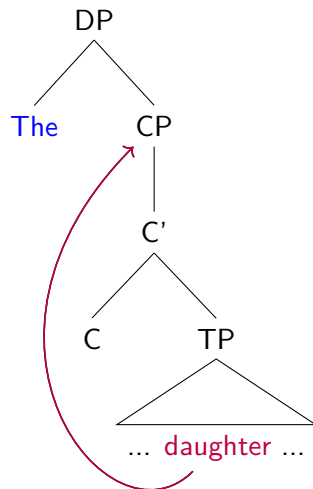
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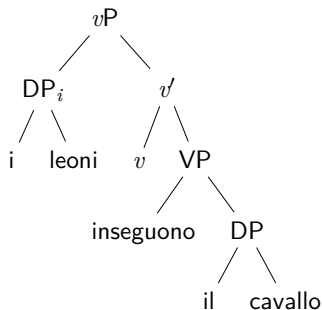
# Postverbal Subjects (Belletti & Leonini 2004)

- (5) Inseguono il cavallo i leoni  
 Chase the horse the lions  
 “The lions chase the horse”

- ▶ the subject DP raises to Spec, FocP
- ▶ The whole  $vP$  raises to Spec, TopP

## Technical details!

- ▶ an expletive *pro* is base generated in Spec, TP



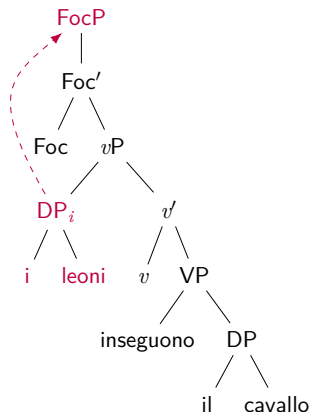
# Postverbal Subjects (Belletti & Leonini 2004)

- (6) Inseguono il cavallo **i leoni**  
 Chase the horse the lions  
 “The lions chase the horse”

- ▶ the **subject DP** raises to Spec, FocP
- ▶ The whole *v*P raises to Spec, TopP

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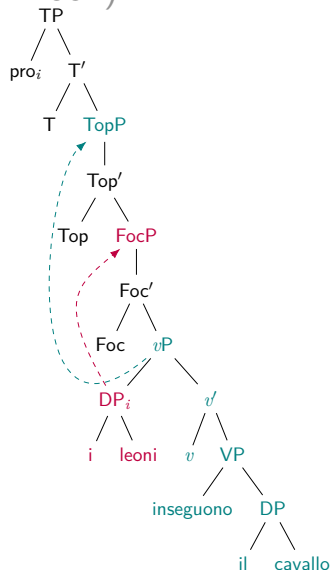
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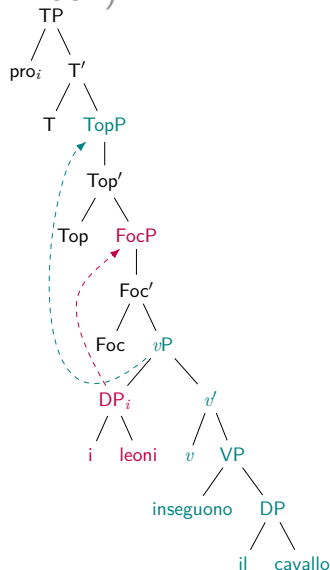
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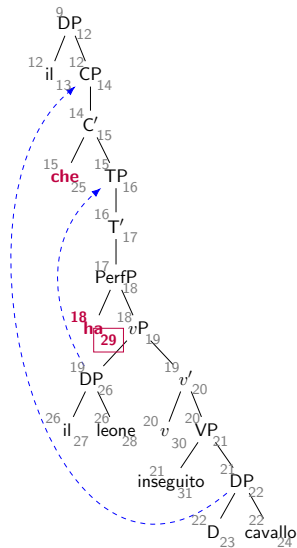
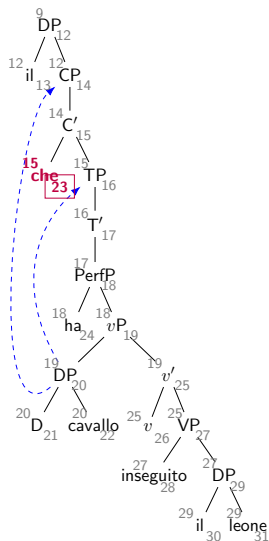
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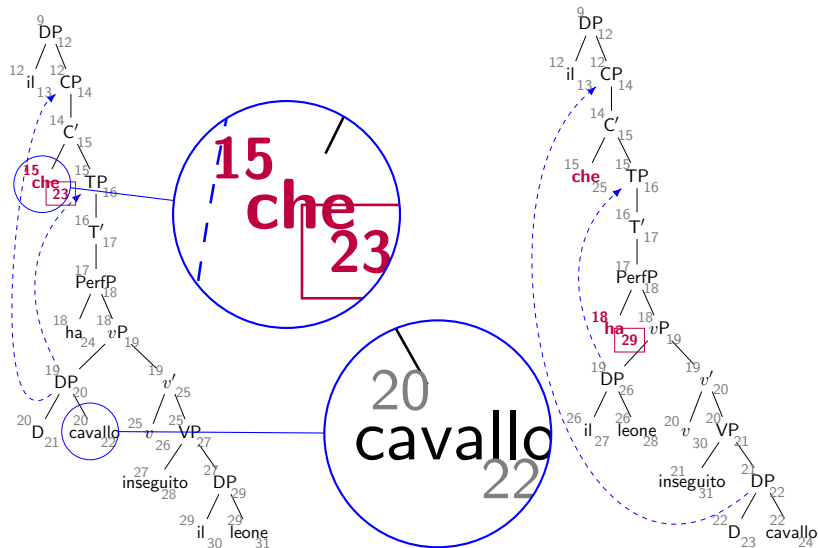


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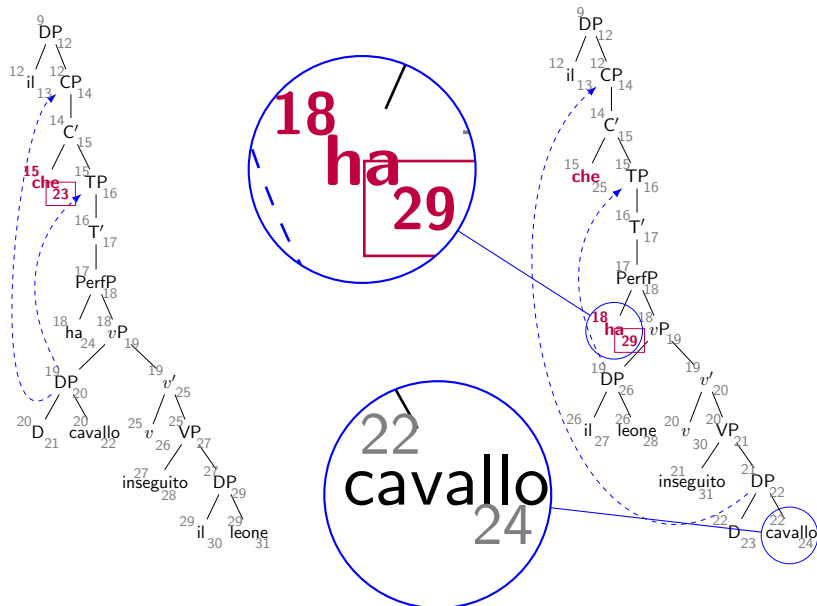




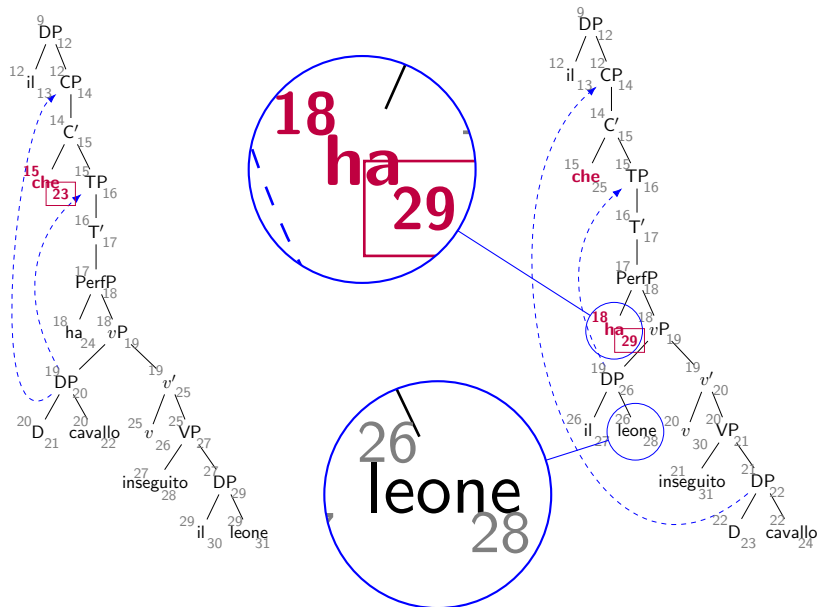
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## Results: SRC &gt; ORC



# Italian Subjects: Probing the Results

Clause Type	MaxT	SumS
obj. SRC	8/ <i>che</i>	18
obj. ORC	11/ <i>ha</i>	24
obj. ORCp	16/ <i>Foc</i>	31
subj. SRC	21/ <i>v'</i>	37
subj. ORC	21/ <i>v'</i>	44
subj. ORCp	28/ <i>v'</i>	56
matrix SVO	3/ <i>ha/v'</i>	7
matrix VOS	7/ <i>Top/Foc</i>	11
VS unacc	2/ <i>vP</i>	3
VS unerg	7/ <i>Top/Foc</i>	11

**Table:** Summary of MAXT (*value/node*) and SUMS by construction. Obj. and subj. indicate the landing site of the RC head in the matrix clause.

# Postverbal Asymmetries: Possible Accounts?

## SRC > ORC

- ▶ DLT, active-filler strategy, Competition model, ...

## ORC > ORC<sub>p</sub>

- ▶ more problematic (e.g., for DLT)
- ▶ can be explained by
  - 1 economy of gap prediction + structural re-analysis;
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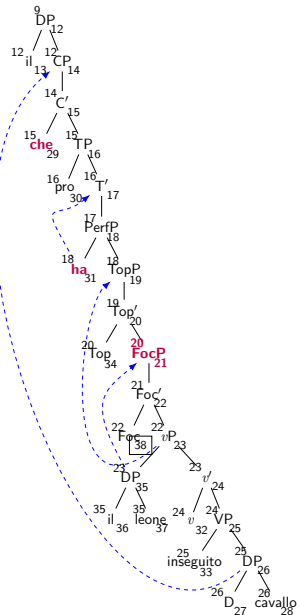
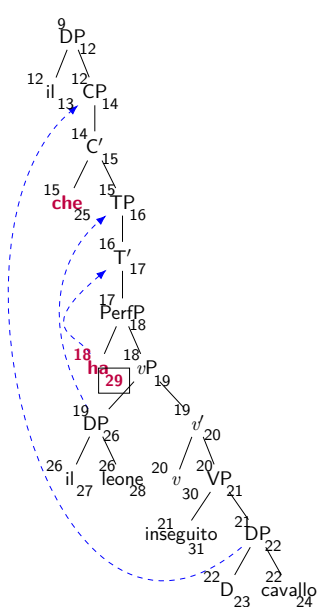
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# Additional Constructions

## ► Ambiguity in Matrix Clauses

(8) Ha chiamato Gio

Has called Giovanni

a. “He/she/it called Gio”

**SVO**

b. “Gio called”

**VS**

## ► Unaccusatives vs. Unergatives

(9) È arrivato Gio

Is arrived Gio

“Gio arrived”

**Unaccusative**

(10) Ha corso Gio

Has ran Gio

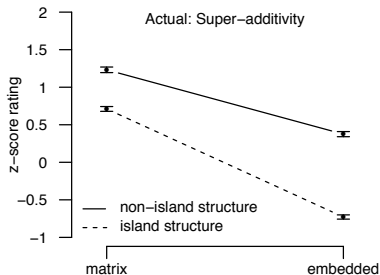
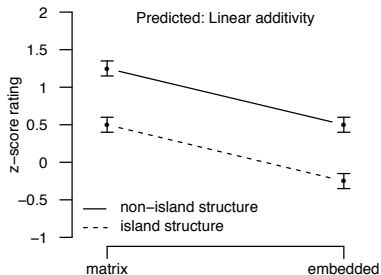
“Gio ran”

**Unergative**

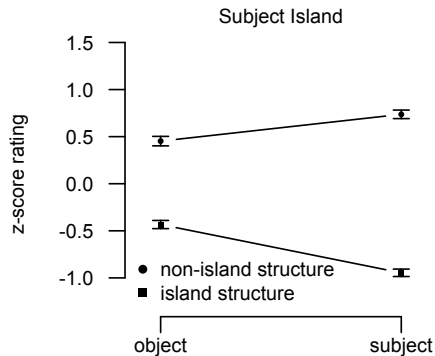
# Gradience in Islands

A factorial design for islands effect:

► GAP POSITION  $\times$  STRUCTURE



# Deriving Pairwise Comparisons



- ▶ Subj | Non Island > Obj | Non Island
- ▶ Subj | Non Island > Obj | Island
- ▶ Subj | Non Island > Subj | Island
- ▶ etc.

# A Caveat on Island Effects

## The Goal

Can **gradience** in acceptability judgments arise from a categorical grammar due to processing factors?

- ▶ Sprouse et al.'s (2012) design is ideal for the MG model.

**But I am not interested in island effects *per se*:**

- ▶ Islands: grammatical or processing effects?  
(Hofmeister et al., 2012a; Sprouse et al., 2012a,b)
  - ▶ hence, not modeling super-additivity
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# Models of Gradience

(At least two) theories of gradience:

- ▶ Gradience incorporated in the grammar  
(Keller 2000; Featherston 2005; Lau et al. 2014)
- ▶ Gradience due to extra-grammatical factors  
(Chomsky 1975; Schütze 1996)

The contribution of formal models?

Quantify what each approach needs to account for the data:

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# Subject Islands

## Case 1:

- (11) a. **What** do you think the speech interrupted ***t***?      Obj | Non Island
- b. **What** do you think ***t*** interrupted the show?      Subj | Non Island
- c. **What** do you think the speech about global warming interrupted the show about ***t***?      Obj | Island
- d. **What** do you think the speech about ***t*** interrupted the show about global warming?      Subj | Island

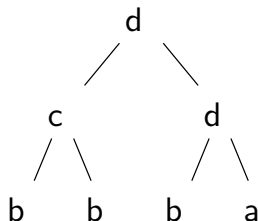
## Case 2:

- (12) a. **Who** ***t*** thinks the speech interrupted the primetime TV show?      Matrix | Non Island
- b. **What** do you think ***t*** interrupted the primetime TV show?      Emb. | Non Island
- c. **Who** ***t*** thinks the speech about global warming interrupted the primetime TV show?      Matrix | Island
- d. **What** do you think the speech about ***t*** interrupted the primetime TV show?      Emb. | Island

# Top-down Parsing + Grammaticalized Constraints?

Graf & De Santo (2019)

**Sensing Tree Automata** (Martens 2006) as a subregular bound on the complexity of syntactic dependencies.

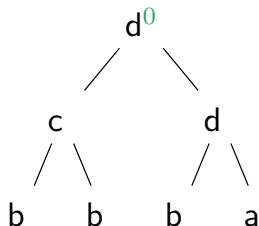


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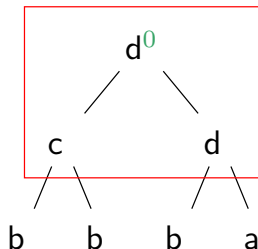


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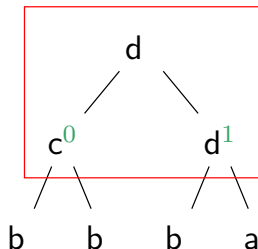
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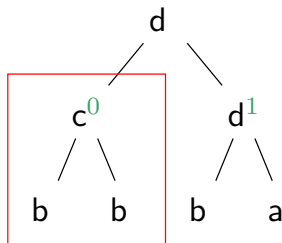
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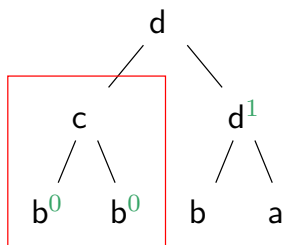


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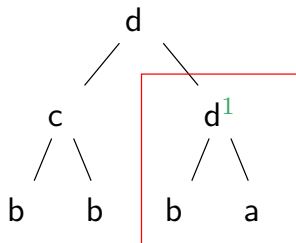
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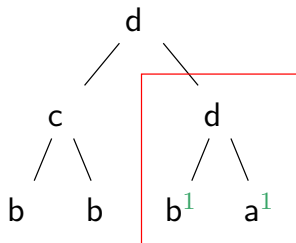
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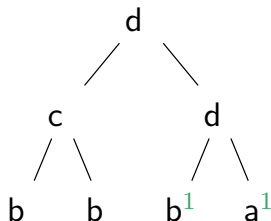


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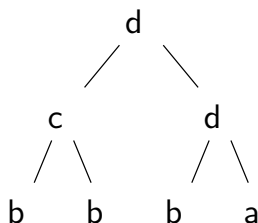


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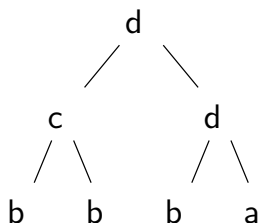
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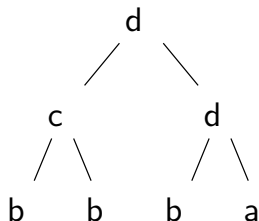
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- ▶ Constraints improve parsing performance by **exponentially reducing** the search space (Stabler 2013)
- ▶ Can be pre-compiled in the MG parse schema as a deterministic **top-down filter** (De Santo & Graf, in prep.)

# Attachment and Relative Clauses (RC)

- ▶ They saw the daughter of the actress that was on the balcony
 

NP <sub>1</sub>	<b>The daughter</b> was on the balcony	HA
NP <sub>2</sub>	<b>The actress</b> was on the balcony	LA

English: **LA** interpretation

- ▶ Late Closure (Frazier 1978),  
Recency (Gibson 1991, Gibson et al. 1996), ...

## Universal locality principles?

- ▶ Spanish: **HA** interpretation
  - ▶ Tuning Hypothesis  
(Cuetos & Mitchell 1988, Mitchell & Cuetos 1991)  
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# A Complex Cross-Linguistic Scenario

## HA vs LA languages?

RC preferences cross-linguistically affected by a variety of factors

- ▶ Syntactic environment  
(Fernandez 2003, Gibson et al. 1996, De Vincenzi and Job 1993)
- ▶ Prosodic effects (Teira and Igoa 2007, Hemforth et al. 2015)
- ▶ Lexical-semantic properties of the DPs  
(MacDonald et al. 1994, Gilboy et al. 1995)
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## Grillo & Costa: Pseudo-RCs in Italian

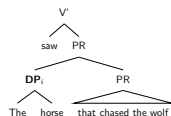
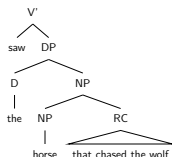
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(I) have seen the grandma of the girl that screaming  
‘I saw [the grandma of the girl that was screaming]’

- ▶ RC: HA
- ▶ RC: LA

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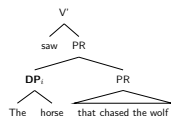
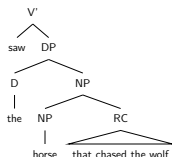
- RC: HA
- RC: LA
- PR



# Grillo & Costa: Pseudo-RCs in Italian

- (13) (Io) Ho visto [la nonna della ragazza che gridava]  
 (I) have seen the grandma of the girl that screaming  
 'I saw [the grandma of the girl that was screaming]''

- ▶ RC: HA
- ▶ RC: LA
- ▶ PR: ~ HA



- ▶ RCs are NP-modifiers and denote properties of entities
- ▶ PRs are complements of VPs and denote events/situations
  - ▶ **Only** compatible with a **HA** reading!

# So What? PRs and Attachment Preferences

- ▶ The grandma of the girl that was screaming
  - ▶ RC: HA
  - ▶ RC: LA
  - ▶ PR: HA

## The Pseudo-Relative First Hypothesis (Grillo & Costa 2014)

All else being equal:

- ▶ When available: PR **preferred over** RC parse (so:  $\sim$  HA)
- ▶ Otherwise: LA RC **preferred over** HA RC parse

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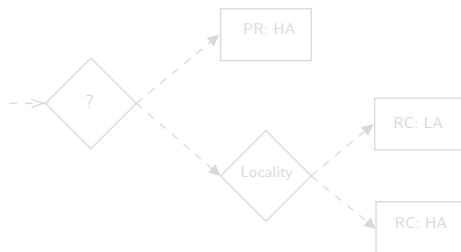
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Syntactic tests (Grimshaw 1990, Chomsky 1992, Chomsky 1995, 2000)

Appear freely with proper names, no relative pronouns, ...

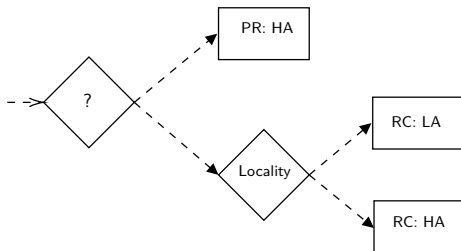
Verb type restrictions

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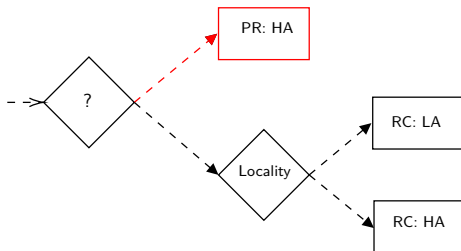


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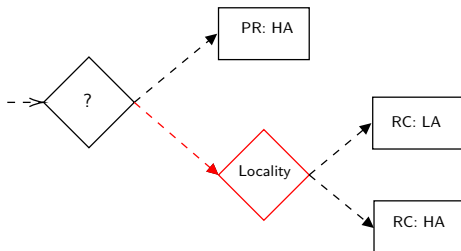


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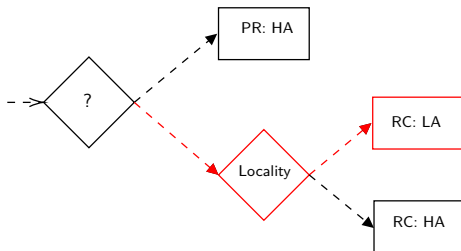


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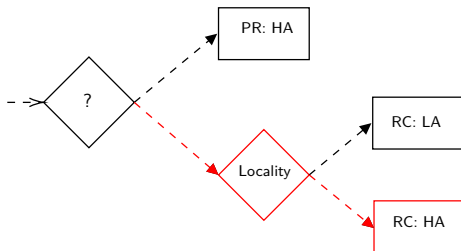


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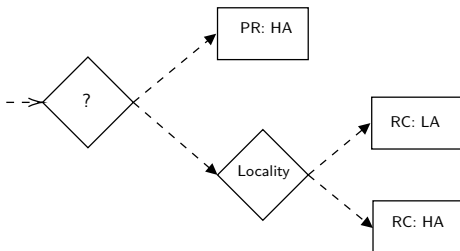


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## Grillo and Costa (2014)

- ▶ The daughter of the actress [that was on the balcony]
  - ▶ RC: HA
  - ▶ RC: LA
  - ▶ PR: (~) HA

Online tool

- ▶ Italian: De Santo & Lee (2022a)
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### (57) Stimuli Experiment II

- a. PR/ RC CONDITION: PR-VERBS  
 Gianni ha visto il figlio del medico che correva.  
*G. saw the son of the doctor running.*
- b. RC ONLY CONDITION: STATIVE VERBS  
 Gianni vive con il figlio del medico che correva.  
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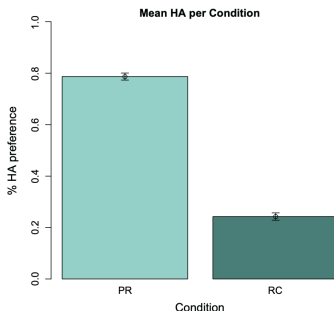
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**Table 6**  
Percentage of high attachment preferences.

Eventive	Stative
78.6%	24.2%



**Fig. 2.** Summary of attachment preference experiment 2.

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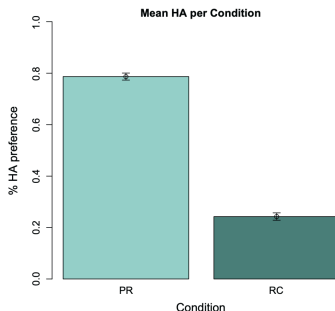
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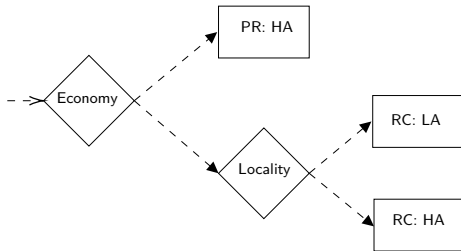


**Fig. 2.** Summary of attachment preference experiment 2.

# PR-First: Why?

## Question

Why should PRs be preferred?



**One Hypothesis: Structural Economy** (Grillo & Costa 2014)

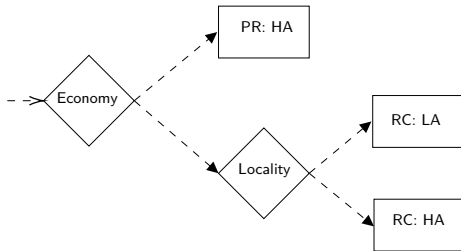
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# Modeling PR-First

## Why should PRs be easier/preferred?

- ▶ Can we evaluate structural economy quantitatively?
- ▶ Do different syntactic choices matter?

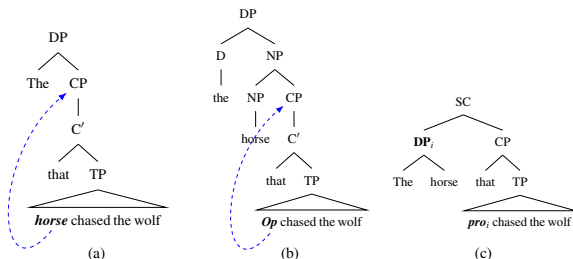


Figure 2: Sketches of the (a) RC with Promotion, (b) RC with Wh-movement, and (c) PR analyses for the sentence *The horse that the wolf chased*.

# Modeling Results (De Santo & Lee, 2022b)

MG Parser: MaxT
Hypothesis
PR > HA
PR > LA
LA > HA

- (15) (Io) Ho visto la nonna della ragazza che gridava  
 (I) have seen the grandma of the girl that screaming  
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- ▶ The PR > HA RC depends on syntactic choices
- ▶ No metric predicts PR > LA RC
- ▶ In sum:  
 No immediate support for a parsing economy explanation
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PR > LA	✗	✗
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# TI/Dr: The Value of Formal Models

## A fully specified model of syntactic cost:

- ▶ Allows evaluation of economy definitions
- ▶ Shows that syntactic choices affect “cost” in unexpected ways
- ▶ Suggest ways to narrow down the space of plausible accounts

## Beyond these results

- ▶ Cross-linguistic and cross-analysis validation
- ▶ A variety of definitions for *cost* in parsing (Boston, 2012)
  - ▶ E.g., # bounding nodes/phases, discourse referents, retrieval
  - ▶ Pragmatic Economy?  
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# A Look at HA Languages (Grillo & Costa 2015)

**Table 4**

Attachment preferences and PR availability.

Language	Attachment	PRs
English	Low	.
Romanian	Low	.
Basque	Low	.
Chinese	Low	.
German (?)	High/Low	.
Russian (?)	High	.
Bulgarian (?)	High/Low	.
Norwegian (?)	Low	✓
Swedish (?)	Low	✓
Spanish	High	✓
Galician	High	✓
Dutch	High	✓
Italian	High	✓
French	High	✓
Serbo-Croatian	High	✓
Japanese	High	✓
Korean	High	✓
Greek	High	✓
Portuguese	High	✓

Figure: Survey of Attachment preferences from Grillo & Costa (2014)

# PRs: Modeling Results 1

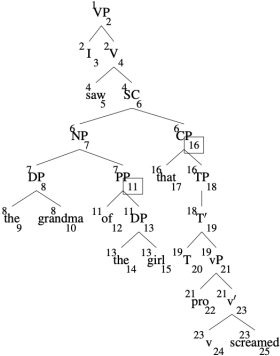


Figure 3: Annotated derivation trees for the Italian sentence *I saw the grandma of the girl that screamed*, according to a pseudo-relative clause analysis. The tree is treated as a VP since additional structure in the matrix clause would be identical across comparisons.

MG Parser		
Hypothesis	Promotion	Wh-mov
PR < HA	✓	Tie
PR < LA	×	×
LA < HA	✓	✓

Table 1: Summary of the predictions made by a *pseudo-relative first* account, and corresponding parser’s predictions based on MAXTENURE, as pairwise comparisons (x < y: x is preferred over y).

MAXT		
	Promotion	Wh-mov
PR	10/CP	
HA	11/that	10/CP
LA	5/that	7/that

Table 2: MAXT values (*value/node*) by construction, with RCs modulated across a promotion and wh-movement analysis.





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